Nonlinear Blend Scheduling via Inventory Pinch-based Algorithm using Discrete- and Continuous-time Models

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This work uses multi-period, inventory pinch-based algorithm with continuous-time model (MPIP-C algorithm¹) for scheduling linear or nonlinear blending processes. MPIP-C decomposes the scheduling problem into (i) approximate scheduling and (ii) detailed scheduling. Approximate scheduling model is further decomposed into two parts: a 1st level model which optimizes nonlinear blend models (with time periods delineated by inventory pinch points), and a 2nd level multi-period mixed-integer linear programming model (which uses fixed blend recipes from the 1st level solution) to determine optimal production plan and swing storage allocation, while minimizing the number of blend instances and product changeovers in the swing tanks. The 3rd level computes schedules using a continuous-time model including constraints based on the short-term plan solution. Nonlinear constraints are used for the Reid vapor pressure in our case studies. Excellent computational performance is illustrated by comparisons with previous approach with discrete-time scheduling model.

Key words:

inventory pinch, nonlinear gasoline blending, discrete-time scheduling model, continuous-time scheduling model

Introduction

Mathematical optimization has become an important supply chain management tool for any contemporary enterprise. Increasing profit margins through better design, planning, and operative decisions across the supply chain represents a huge opportunity in the more than ever competitive economic market, especially in a global scale. Industrial and academic researchers have been working intensively in the process systems engineering area, and several advancements have been made in the optimization field, from new mathematical models, more efficient solution algorithms, use of more powerful computing machines and with parallel capabilities, and the development of different optimization frameworks.

A supply chain is composed of the following elements: procurement and storage of raw materials, facilities and processes to transform the raw materials into intermediate and final products, storage of these products and its distribution to warehouses or to the final customers. Operating the complete supply chain structure in the best possible manner (i.e. maximizing profit or minimizing cost) involves making decisions at different levels along the supply chain network. Production planning determines the production targets of each different product along a defined planning horizon (usually ranging from a few months to 2 years), for the entire supply chain, for each different production facility, or for each production line or unit. Production scheduling determines the best operating sequences and the best operating conditions to achieve the inventory and production targets determined by the production plan. Scheduling is done on smaller time horizons (e.g. days or weeks), and includes more operational rules and constraints than planning models. Fig. 1 shows how the length of the time horizon and model accuracy changes, depending on the spatial or time scale, under a hierarchical production planning framework.



Fig. 1 – Hierarchical production planning with respect to a) spatial scale, and b) time scale [Adapted from Castillo and Mahalec¹⁷]

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Computation of optimal production plans is usually based on linear programming (LP) or successive linear programming (SLP) models^{2,3,4} since these approaches have proven to be robust and provide good answers under a variety of circumstances. Production planning models are constructed by dividing the time horizon in a number of periods, the length of which is usually set equal to some calendar unit (e.g. monthly, or quarterly periods). Such approach leads to models which grow in size linearly with the number of periods. If the models are nonlinear, the likelihood of encountering convergence problems increases significantly as the problem size increases. However, formulation of planning models with nonlinearities is becoming more spread in practice^{4,5,6,7} in order to compute more accurate solutions and increase profitability. Scheduling is in many cases a NP-complete^{8,9} or NP-hard¹⁰ problem, which means that there is no polynomial-bounded algorithm to solve it, even if the underlying supply chain models are linear. Process plants are nonlinear but the usual practice for scheduling is to approximate the system behavior by linear models.^{2,11,12,13} Recent advances have made it possible to use nonlinear models for some scheduling problems.14,15

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MPIP-C algorithm¹ enables use of nonlinear models to solve scheduling problems for plants which produce multiple products by switching from producing one product to another. An example of such system is gasoline blending. The first step is to compute an approximate scheduling solution which imposes some constraints on the detailed scheduling problem, thereby simplifying it and reducing the number of integer variables: it also enables faster solution of detailed scheduling problems by providing additional constraints. MPIP-C algorithm uses inventory-pinch based two-level approach to solve the approximate scheduling problem^{16,17} based on nonlinear blending models. The algorithm:

(i) Computes an approximate schedule based on a nonlinear blend model, such that the there is a minimum number of optimal blend recipes along the planning horizon,

(ii) Minimizes the total number of blend instances, and

(iii) Allocates swing tankage.

Solution of the approximate planning model provides additional constraints for the 3rd level continuous-time scheduling problem. If the 3rd level scheduling problem is infeasible, the algorithm resolves a modified approximate scheduling problem, and iterates until a feasible optimal solution is found. We use gasoline blending as an example of the algorithm application. This paper is organized as follows: First, a brief review on prior work on blend planning and scheduling, then we present the problem statement, which is followed by the description of our decomposition approach, the mathematical models used, the MPIP-C algorithm steps, numerical results and conclusions.

Related prior work

In this section, a brief summary of previous works on blend planning and scheduling is presented.

Mendez et al.³ presented an algorithm to schedule blending operations including blend recipe determination. In order to approximate nonlinear quality constraints, they use linear constraints with correction factors. The algorithm iterates until the correction factors converge. The sequencing problem is avoided since it is assumed that each blender produces only one particular gasoline grade.

Li et al.¹⁸ developed a continuous-time mixed integer linear programming (MILP) model with a common global time grid for all units. The model includes blend recipe optimization, and operational features found in industrial practice such as parallel non-identical blenders, multipurpose tanks, inventory constraints, blender capacity constraints, and order delivery scheduling. Li and Karimi¹³ extended the model from Li et al.¹⁸ in order to incorporate blender setup times and consider the case for simultaneous receipt and delivery by product tanks. Li and Karimi¹³ used a unique time grid for the time slots of each unit (i.e. tanks and blenders). Solving these models for real-life scale problems (e.g. 8-day horizon, three blenders, and more than 25 orders) to optimality requires large execution times (more than 12 hours for their case studies).

Kolodziej et al.¹⁵ formulated a discrete-time mixed integer nonlinear programming (MINLP) model to solve the pooling problem including inventory, flow, and quality constraints. They developed three different procedures to solve the MINLP problem to global optimality. Two of those algorithms use a radix-based discretization technique to discretize one variable in the bilinear terms and obtain MILP relaxations, and one of them computes better solutions and in less time than commercial MINLP solvers such as BARON and GloMIQO, for their case studies and despite the increment in the number of binary variables in the model.

Glismann and Gruhn¹⁹ developed a two-level method to solve the blend scheduling problem. First, a discrete-time NLP model computes blend recipes and production targets. Then a discrete-time MILP scheduling model, based on a resource-task-network representation, is solved. If the MILP is infeasible, the algorithm re-computes the blend recipes by re-solving the NLP model with extra constraints. Thakral and Mahalec²⁰ presented an iterative algorithm that optimizes blend recipes using a multi-period MILP planning model, then minimizes blender switches through the use of a genetic algorithm, and subsequently detects infeasibilities via agent-based simulation. The algorithm is repeated until a feasible solution is found.

Inventory pinch analysis in production planning and scheduling

Singhvi and Shenoy²¹ presented a pinch analysis approach to solve an aggregate production planning problem. They constructed composite curves for the demand and production amounts in order to locate the pinch as the point where both curves touch. The idea is to determine the composite production curve that meets the demand and the given inventory policy. Production targets are determined directly from the composite curves and imposed as constraints into a MILP model that minimizes the material, inventory, and labor costs, subject to material balance equations and production capacity constraints. Singhvi et al.²² extended the work from Singhvi and Shenoy²¹ in order to handle multiple products and solve the product sequencing problem based on some heuristic rules and assuming that the demand is met only at the end of the horizon. Ludwig et al.²³ applied the pinch analysis of Singhvi and Shenoy²¹ to a process with seasonal supply, and they included the constraint that the composite production curve must not cross either the composite demand curve or the composite supply curve. Foo et al.²⁴ implemented the algebraic technique equivalent to the graphical pinch methodology from Singhvi and Shenoy²¹ for a single product process, and included minimum and maximum product inventory constraints and the capability of scheduling a plant shut down.

Castillo et al.¹⁶ defined an inventory pinch as the point in time where the composite total demand (CTD) curve touches the composite average total production curve (CATP). The CATP curve can be defined as the concave envelope of the CTD curve, with the difference that the CATP curve starts at the total initial product inventory. Fig. 2 shows an example with two inventory pinch points. In contrast with previous approaches to solve planning problems using composite curves, the CATP curve does not represent the actual production rates; it is only used to locate the pinch points, as well as the minimum production volumes to satisfy the demand in each interval delineated by pinch points. The idea is that between pinch points, the same optimal blend recipes can be used to generate a feasible blend plan. This is not always the case due to other operational constraints, and Castillo et al.¹⁶ developed an iterative approach to eliminate such infeasibilities.



Fig. 2 – Two inventory pinch points on the cumulative curves

Castillo et al.¹⁶ introduced a two-level inventory pinch-based decomposition approach to solve multi-period gasoline blend planning models with nonlinear blending rules. The blend recipes are computed at the first level by solving a discrete-time NLP model which only considers the material balance equations around the blenders and storage tanks, the linear and nonlinear quality equations, the minimum and maximum inventory and production capacity constraints, and product quality specifications. Then, these recipes are fixed at the second level which consists of a discrete-time MILP model. The integer variables are required to enforce minimum production thresholds at each time period. The number of time periods at the first level is delineated by the inventory pinch points, and changes in the quality and price of blend components, while the number of time periods at the second level is determined by the planner/scheduler. For the case studies presented by Castillo et al.¹⁶, this approach computes solutions that are optimal or close to the optimum, and with rapid execution times compared with MINLP solvers. Castillo and Mahalec^{17,25} extended the algorithm from Castillo et al.¹⁶ to solve blend scheduling problems by introducing a third level to solve the scheduling problem using a discrete-time MILP model. Most recently, Castillo and Mahalec¹ developed a continuous-time model to solve the third level more efficiently.

Problem statement

Given a scheduling horizon [0, H], a blending system constituted of storage tanks and blenders (see Fig. 3 for an example), and sets of blend components, products, and delivery orders which must be fulfilled during specific time delivery windows along the horizon, the objective is to minimize the total cost which consists of the cost of the blended materials (i.e. the blend cost) and the switching costs comprised of the number of different blend runs, product changeovers in the storage tanks, and



Fig. 3 – Sample blending system

number of deliveries from different tanks to the same order. The cost, quality properties, initial inventories, and flow rates into the system of the blend components are known. Minimum and maximum product quality specifications are given. Initial product inventories are known and on specification. Blend components have dedicated storage tanks. Storage tanks for the finished products can be dedicated tanks or swing tanks (i.e. they can store different products, but not at the same time). Product changeover times are negligible for swing tanks. All storage tanks have minimum and maximum capacity constraints. Parallel non-identical blenders are considered, with minimum and maximum blending capacities. Minimum blend size, minimum blend length, and minimum setup time constraints are assumed for each blender and they are product-dependent. Perfect mixing is assumed to occur in the blenders and a blender can only feed one product tank at any time, since this is industrial practice. Each order involves only one product (one original order involving different products can be broken into orders of each specific product).

It is required to determine the blend recipes, the production sequence of each blender, the blending rates of each blend run, the delivery sequence of each product tank, the start and end times of the blend runs and delivery runs, the product allocation of swing tankage, and the inventory profiles of all tanks along the horizon.

Decomposition strategy

In this work we use the decomposition framework from Castillo and Mahalec^{1,25}. It is assumed that a long-term (e.g. twelve months) production planning model has been optimized for the refinery or the gasoline blend system. In addition, it is assumed that the long-term plan determines which feedstocks are to be processed, which products are produced, and the total amount for each of them, respectively. Results of the long-term plan are used to optimize a short-term discrete-time multi-period approximate scheduling model (e.g. thirty days), which in turn provide constraints for a continuous-time scheduling model (see Fig. 4).

Approximate scheduling

The purpose of the approximate scheduling model is to minimize the production costs or to maximize the profit for a given selection and quan-



Fig. 4 – Three-level decomposition approach

tities of the feedstocks. In addition, the approximate scheduling model:

- Determines how much to produce of each product and each time period.

 Manages allocation of the swing storage capacities; it is assumed that a swing storage capacity can be re-allocated only at the beginning of each period.

- Minimizes the number of instances of different operating modes for each multi-mode unit, e.g. maximum gasoline or maximum diesel for an FCC unit, or number of different grade gasoline blenders for a gasoline blender. In order to eliminate instances of minute production for any operating mode, a minimum threshold production constraint is specified for each production unit.

Another difference between approximate scheduling and detailed scheduling models is that tasks and resources are still aggregated in some way at the short-term planning level. Therefore, solution of approximate scheduling determines a production and inventory profile which is feasible only at the period boundaries (e.g. end of each day).

Objective function at this level includes in general case the costs of carrying the inventories and the switching costs associated with the discrete variable (decisions). Cost of raw materials plus operating costs computed at this level are the same as at the top level, since the operating modes and the total feed amounts are fixed by the top level.

Detailed scheduling

Detailed scheduling model allows only one task in any production unit at any given time, thus guarantying a feasible solution along the entire horizon. Objective function at the scheduling level includes only the switching costs and in general case the costs of transitions from one mode of operation to another. Solution of the approximate scheduling model (i.e. approximate scheduling model) leads to a neighborhood where the optimal schedule is located. This neighborhood is described to the detailed scheduling task in terms of target inventories at the end of each day, operating modes at which each process unit needs to operate during each day, etc. From these data, computation of the best schedule can proceed in several different ways, for example:

a) Determine operating sequence with a minimum number of switches via some evolutionary algorithm and verify its feasibility via simulation (e.g. Thakral and Mahalec²⁰).

b) Use fine-grid discrete-time MILP scheduling model (e.g. Castillo and Mahalec²⁵).

c) Solve a continuous-time MILP scheduling model (e.g. Castillo and Mahalec¹).

In this work, we use option c), since the continuous-time model has a smaller size than its corresponding discrete-time version, thus allowing solving of problems in less time. When using the constraints imposed by the approximate scheduling level, the detailed scheduling level is solved much faster. However, due to the consequent reduction in the feasible solution set, optimality of the computed schedule with respect to the original problem (i.e. no constraints from the approximate scheduling level) is not guaranteed, although the optimality gap is expected to be very small. One way to improve this solution is to use it as a starting point for the scheduling model that includes quality constraints and allow the blend recipes to differ from those previously computed at the short-term planning level. The disadvantage is that the resulting MILP or MINLP model may require prohibitive execution times in order to close the optimality gap. Future work will be dedicated to address this issue and compute proven optimal solutions with respect to the original problem.

Mathematical models

In this section, the mathematical models are described. Due to the large number of equations, only the nonlinear equations for Reid vapor pressure (RVP) used in this work are here shown. The reader is encouraged to look at the references where the complete models are described in detail.

1st level model¹⁷ (discrete-time LP or NLP)

The 1st level determines the optimal blend recipes that will be fixed at the next levels. The time periods of this model are the L1-periods. The objective function minimizes the blend cost and the cost associated with slack variables. Slack variables are included in the inventory balances and their penalty coefficients in the objective function are greater than the cost coefficients of the blend components. Therefore, if a problem has a physically feasible solution, the slack variables will be equal to zero. If a problem has no physically feasible solution, the solver will compute a numerical feasible solution with some non-zero slack variables. The values of the blending capacity, component supply, and product demand are the corresponding aggregated values for each of the L1-periods. In addition, individual product tanks are aggregated into product pools, and individual blenders are lumped into a single one

- Blend recipe optimization -

min BlendCost_{L1} + SlackCost_{L1}

s.t.

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Inventory balances (component tanks, product pools) Inventory constraints (component tanks, product pools) Quality constraints (linear and nonlinear)

Maximum production capacity (lumped blenders)

The solution of the 1st level model is a lower bound of the global blend cost since the volumes to be blended in each L1-period are the minimum amount required to fulfill the demand.

The nonlinear quality constraints used in this work are presented next. Equation (1) and (2) define the blend recipes. Equation (3) was formulated based on the nonlinear blending rule used by Singh et al.²⁶ Equation (4) represents the minimum and maximum product quality specifications for RVP property.

$$r(i,p,k) = \frac{V_{comp,L1}(i,p,k)}{V_{blend,L1}(p,k)} \quad \forall i,p,k \ge 1 \quad (1)$$

$$\sum_{i} r(i, p, k) = 1 \quad \forall p, k \ge 1$$
 (2)

$$Q_{pr}(p, \text{'RVP'}, k) = \left[\sum_{i} Q_{bc}(i, \text{'RVP'}, k)^{1.25} \cdot r(i, p, k)\right]^{0.8}$$
$$\forall p, k \ge 1$$
(3)

$$Q_{pr}^{\min}(p,e) \le Q_{pr}(p,e,k) \le Q_{pr}^{\max}(p,e)$$
$$\forall e = \{\text{RVP}\}, p,k \ge 1$$
(4)

2nd level model^{1,25} (discrete-time MILP)

The 2^{nd} level computes the blend plan, delivery plan, and service allocation of swing tanks. The time periods of this model are the L2-periods. The blend plan determines how much to blend of each product, in which blender, and in each L2-period. The delivery plan defines how much product to send from each individual product tank to each specific order and in which L2-period. The allocation of swing tanks establishes which product can be stored in each individual product tank and in which L2-periods.

The 2nd level model is linear since the blend recipes from the 1st level are not computed at this level (i.e. the blend recipes of each L1-period are fixed in the corresponding L2-periods). Equations regarding individual product tanks and individual blenders are included. Moreover, constraints such as minimum blend size, minimum blend length, and minimum setup time are incorporated. The values of the blending capacity, component supply, and product demand are the corresponding aggregated values for each of the L2-periods. The individual blenders can produce more than one product in each L2-period. A swing tank can only store one specific product during a L2-period.

The 2^{nd} level model is solved in two phases: feasibility of the blend recipes is checked first, and then a solution with minimum number of switches is computed. The reason to do this is to detect inventory infeasibilities (i.e. non-zero slacks) rapidly.

The 2nd level model for feasibility check has slack variables in the inventory balances and the objective is to minimize such variables. If a feasible operation can be obtained using the blend recipes from the 1st level, inventory slack variables will be zero at the solution of the 2nd level; otherwise, the inventory slacks will show which specific products, by how much, and in which L2-periods they cannot be produced in the amounts required. In order to extend the use of a given blend recipe, the penalty coefficients for the slack variables must decrease along the time horizon as fast as possible and a significant change must take place after each L1-period boundary.

– Feasibility check of blend recipes from 1st level –

min SlackCost_{1,2}

s.t.

Fixed recipes (from 1st level)

Product inventory targets (from 1st level)

- Inventory balances (component tanks, product pools, product tanks)
- Inventory constraints (component tanks, product tanks)

Maximum production capacity (individual blenders)

- Minimum product-dependent blend size (individual blenders)
- Minimum product-dependent run length (individual blenders)
- Minimum product-dependent setup time (individual blenders)
- Maximum delivery rates of each individual product tank

When the solution of this phase has inventory infeasibilities, the algorithm will subdivide the required L1-period at the time corresponding to the end boundary of the L2-period with the first infeasibility. Then, the 1st level model is re-solved and a new set of blend recipes is computed.

The 2nd level model for minimizing switching costs (i.e. number of blend runs, number of product changeovers in the swing tanks, and number of de-

livery runs from different tanks to the same order) does not include any slack variables.

- Computing blend plan, delivery plan, and swing tank allocation with minimum number of switches -

min SwitchingCost₁,

s.t.

 $\begin{aligned} & \text{SwitchingCost}_{\text{L2}} = \text{SwitchBlenderCost}_{\text{L2}} + \\ & + \text{SwitchTankCost}_{\text{L2}} + \text{SwitchDeliverCost}_{\text{L2}} \end{aligned}$ Fixed recipes (from 1st level)

Product inventory targets (from 1st level)

Inventory balances (component tanks, product

- pools, product tanks)
- Inventory constraints (component tanks, product tanks)

Maximum production capacity (individual blenders)

- Minimum product-dependent blend size (individual blenders)
- Minimum product-dependent run length (individual blenders)
- Minimum product-dependent setup time (individual blenders)
- Maximum delivery rates of each individual product tank

3rd level model¹ (continuous-time MILP)

The 3rd level determines:

- Start and end times of all tasks,
- Production sequence of each blender,
- Blending rates for each blend run,
- Delivery sequence of all product tanks, and
- Delivery rates for each delivery run.

The blend recipes from the 1st level, the swing tank allocation, and the delivery and blend plans from the 2nd level are fixed. Using information from the 2nd level decreases the search space and the model size at the 3rd level. The time slots are unit slots, meaning that each unit (i.e. component tanks, blenders, and product tanks) have their own specific time grid. From here on, the term time slot and unit slot will be used interchangeably. The 3rd level is formulated as a continuous-time model in order to have a smaller model size with less discrete variables than a corresponding discrete-time model. The 3rd level model is based on the continuous-time model presented by Li and Karimi13 which has been modified by modifying some constraints and adding new constraints in order to avoid infeasible solutions¹.

Only one specific product can be produced by a blender in a given time slot, as well as only one product can be stored in a swing tank. The 3rd level model includes slack variables in the inventory balances and demand constraints. The penalty profile for the slack variables decreases along the scheduling horizon. For large-scale problems, the scheduling horizon can be divided in various subintervals, denoted as L-intervals. Then, the 3rd level MILP model is solved sequentially for each L-interval. The boundaries of the L-intervals must coincide with the boundaries of some L2-periods to enable the inventory levels computed at the 2nd level to be fixed at the start and end boundaries of the L-intervals

Similarly as with the 2nd level, the 3rd level is solved in more than one phase. First, a feasibility check is carried out in order to determine if the blend recipes from the 1st level and the constraints from the 2nd level can produce a feasible schedule, and if the number of time slots can produce a feasible solution. When the feasibility check does not find a physically feasible schedule, the slack variables have non-zero values at the solution. If that is the case, the required L1-period is subdivided at the time corresponding to the end boundary of the L2-period associated with the time slot containing the first infeasibility. After a feasible solution is found, then an optimization phase computes the production and delivery sequences with minimum number of blend runs and delivery runs. Finally, with the production and delivery sequences fixed, blending rate variations are minimized. The 3rd level model for the feasibility phase is denoted as F-Sim-RD-PlanTDBR-feas, the one for the optimization phase is referred to as F- SimRD-PlanTDBR-opt, and the model to reduce variations in the blending rates is designated as F-SimRD-PlanTDBR-adj. The letter F means fixed recipes, SimRD indicates that product tanks can receive and deliver material simultaneously, PlanTDBR signifies that the plan computed at the 2nd level is enforced, and the last word indicates if it corresponds to the feasibility phase (feas), optimization phase (opt), or the adjustment phase (adj) to reduce blending rate variations.

 Feasibility check of blend recipes from 1st level and constraints from 2nd level –

Model F-SimRD-PlanTDBR-feas

min SlackCost₁₃

st

Fixed recipes (from 1st level)

Product inventory targets (from 1st and 2nd levels)

Fixed swing tank allocation (from 2nd level)

- Blend plan constraints (from 2nd level)
- Inventory balances (component tanks, product tanks)
- Inventory constraints (component tanks, product tanks)

Maximum production capacity (individual blenders)

- Minimum product-dependent blend size (individual blenders)
- Minimum product-dependent run length (individual blenders)
- Minimum product-dependent setup time (individual blenders)
- Maximum delivery rates of each individual product tank

 Computing production and delivery sequences with minimum number of switches –

Model F-SimRD-PlanTDBR-opt

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min BlendCost_{L3} + SwitchingCost_{L3} + SlackCost_{L3} s.t.

- $SwitchingCost_{L3} = SwitchBlenderCost_{L3} + Switch DeliverCost_{L3}$
- Fixed recipes (from 1st level)

Product inventory targets (from 1st and 2nd levels)

Fixed swing tank allocation (from 2nd level)

Blend plan constraints (from 2nd level)

- Inventory balances (component tanks, product tanks)
- Inventory constraints (component tanks, product tanks)
- Maximum production capacity (individual blenders)
- Minimum product-dependent blend size (individual blenders)
- Minimum product-dependent run length (individual blenders)
- Minimum product-dependent setup time (individual blenders)
- Maximum delivery rates of each individual product tank

 Minimizing blending rate variations on each blend run –

Model F-SimRD-PlanTDBR-adj

min BlendRateVariations

s.t.

BlendRateVariations = $\sum_{bl,n}$ VolumeDifference_{L3}(bl,n) VolumeDifference_{L3}(bl,n) \geq AvgBlendRate(bl,n).

BlendLength_{L3}(*bl*,*n*) – VolumeBlended_{L3}(*bl*,*n*)

VolumeDifference $(bl,n) \ge$ VolumeBlended (bl,n)

- AvgBlendRate(bl,n) ·BlendLength_{L3}(bl,n)

Fixed production sequence

- Fixed delivery sequence
- Fixed recipes (from 1st level)
- Product inventory targets (from 1st and 2nd levels)
- Fixed swing tank allocation (from 2nd level)
- Blend plan constraints (from 2nd level)

Inventory balances (component tanks, product tanks) Inventory constraints (component tanks, product

- tanks)
- Maximum production capacity (individual blenders)
- Minimum product-dependent blend size (individual blenders)
- Minimum product-dependent run length (individual blenders)
- Minimum product-dependent setup time (individual blenders)
- Maximum delivery rates of each individual product tank

Description of the MPIP-C algorithm

The multiperiod inventory pinch algorithm with a continuous-time scheduling model at the 3rd level for scheduling of blend operations is described next. Although it was developed for gasoline blending, it can be used in any blending process where the quality properties of the blend components are known in advance.

Step 1) Determine the pinch point(s) location on the cumulative curves (CTD and CATP).

Step 2) Set the number of *L1*-periods. The boundaries of these time periods are delineated based on:

- Inventory pinch points.

- Changes in the quality of blend components.
- Changes in the cost/price of components/ products.

Step 3) Set the number of *L2*-periods. The boundaries of these time periods are based on:

- Boundaries of the *L1*-periods.

Variations in supply profile of blend components.

- Time delivery windows for the demand orders.

- Expected time that a swing tank remains in one specific service.

- Time to produce the minimum allowed blend run.

Step 4) Solve the 1st level model. If slack variables have non-zero values at the solution, the problem is infeasible; otherwise, go to Step 5.

Step 5) Solve the 2^{nd} level model for the feasibility check.

Step 6) Continue to Step 8 if solution from Step 5 has all slack variables with zero values; otherwise, go to Step 7.

Step 7) Determine the *L2*-period with the first non-zero slack variable along the horizon and use its end boundary to delineate a new boundary at the 1^{st} level. Return to Step 4.

Step 8) Solve the 2nd level model for minimizing switching costs.

Step 9) Set the number of time slots (*N*) assigned to the scheduling horizon.

Step 10) Solve model F-SimRD-PlanTD-BR-feas.

Step 11) If all slack variables are equal to zero, go to Step 13; otherwise, add more time slots and return to Step 10.

If the number of time slots exceeds the maximum limit, subdivide an *L1*-period and go back to Step 4.

Step 12) Solve model F-SimRD-PlanTDBR-opt.

Step 13) Fix the production and delivery sequences and compute the average blending rates of each blend run.

Step 14) Solve model F-SimRD-PlanTDBR-adj to minimize blending rates variations across a blend run constituted by more than one time slot.

Numerical results

All problems have been solved on DELL PowerEdge T310 (Intel® Xeon® CPU, 2.40 GHz, and 12 GB RAM) running Windows Server 2008 R2 OS. The data for all problems appear in Castillo and Mahalec²⁵. Table 1 shows the physical size of these problems, and Table 2 shows the size of the corresponding continuous-time MILP scheduling model used at the 3rd level. The 3rd level was solved in five L-intervals (i.e. subintervals of the scheduling horizon, one model instance for each one), and Table 2 only shows the size of the largest model. For all case studies, the scheduling horizon is 14

Table 1 – Attributes of the case studies							
Case Study ID	# Blenders	# Orders	# Quality properties	# Products	# Product tanks (swing tanks)		
8	1	36	8	3	6 (3)		
9	1	36	8	3	6 (3)		
10	1	37	8	3	6 (3)		
11	2	37	8	3	6 (3)		
12	2	35	8	3	6 (3)		
13	2	37	8	3	6 (3)		
14	3	37	8	3	6 (3)		

 Table 2 – Size of model F-SimRD-PlanTDBR-opt for the largest model at the 3rd level

Case Study	# Slots (Entire horizon)	# Slots (Largest model)	# Equations	# Continuous Variables	# Binary Variables
8	47	11	3,755	2,267	215
9	51	16	5,525	3,206	316
10	63	15	4,974	3,007	284
11	43	11	5,418	2,599	384
12	39	10	5,064	2,423	357
13	46	11	5,613	2,743	393
14	44	11	7,336	3,124	564

days, the first L-interval is constituted of the first 4 days, the second L-interval spans day 5 to day 7, the third L-interval is composed of day 8 and 9, the fourth L-interval spans day 10 to day 12, while day 13 and 14 constitute the fifth L-interval. The Reid vapor pressure is the only nonlinear quality property considered.

Table 3 – Results from MPIP-C and MPIP^a algorithms. Solvers: IPOPT and CPLEX 12.3

Case Study	Algorithm/ MINLP solver	# <i>L</i> -intervals at the 3 rd level	Obj. Func. Value (\$)	Blend cost (\$)	# Blend runs	# Delivery runs	CPU time (s)	Gap (%)
0	MPIP-C	5	38,483.4	37,943.4	17	40	298.4	0.79
0	MPIP ^a	7	38,498.4	37,943.4	17	43	981.0	0.82
0	MPIP-C	5	39,304.2	38,754.2	18	38	124.0	0.79
9	MPIP ^a	7	39,394.2	38,754.2	21	44	3,477.0	1.03
10	MPIP-C	5	39,020.2	38,405.2	21	39	593.2	0.96
10	MPIP ^a	7	39,050.2	38,405.2	21	45	2,430.0	1.03
11 -	MPIP-C	5	38,935.2	38,405.2	17	38	139.3	0.74
	MPIP ^a	7	39,035.2	38,405.2	20	46	5,106.0	1.00
12	MPIP-C	5	38,633.4	38,073.4	19	36	77.4	0.85
12	MPIP ^a	7	38,733.4	38,073.4	23	40	3,666.0	1.11
12	MPIP-C	5	38,384.5	37,784.5	20	40	341.5	0.93
13	MPIP ^a	7	38,519.5	37,784.5	25	47	1,923.0	1.29
14 -	MPIP-C	5	38,421.4	37,796.4	22	37	206.1	1.00
	MPIP ^a	7	38,546.4	37,796.4	26	46	2,455.0	1.33

^aMPIP scheduling algorithm from Castillo and Mahalec²⁵



Fig. 5 – Production sequence, MPIP-C solution for case study 14



Fig. 6 – Delivery sequence, MPIP-C solution for case study 14

Table 3 presents the results obtained by MPIP-C algorithm and compares them with those obtained by MPIP algorithm (from Castillo and Mahalec²⁵) which uses a discrete-time MILP scheduling model at the 3rd level. It can be observed that MPIP-C algorithm outperforms MPIP algorithm in both solution quality and execution time. This is due to the

reduction in the model size by using a continuous-time scheduling model, which allows subdivision of the scheduling horizon into larger L-intervals and solving them more efficiently.

For illustration purposes, solution for case study 14 is presented. Fig. 5 and Fig. 6 show the production and delivery sequences, respectively.

Conclusions

This work uses MPIP-C algorithm for scheduling of multipurpose systems such as blending operations in petroleum refineries. MPIP-C scheduling algorithm decomposes the problem into three different decision levels. By using information from the upper levels, good quality schedules can be computed with short execution times.

The MPIP-C algorithm uses the inventory pinch concept to compute optimal blend recipes at the 1st level. This computation can be based on either linear or nonlinear models. The 1st level uses aggregated representation of the system, i.e. all blenders are treated as a lumped capacity, all production and demands are lumped across the time periods delineated by the inventory pinch points. Blend recipes computed at the 1st level are employed at the 2nd level to compute an optimal production plan which includes allocation of swing inventories and association of product deliveries with specific tanks. Scheduling of blend runs and delivery liftings is carried out at the 3rd level using a continuous-time MILP model. Solution from the upper levels provides additional information which helps reduce the model size and computational times to solve the 3rd level model.

Seven case studies were presented. MPIP-C computes better solutions and in less time than the previously published MPIP algorithm. The use of a continuous-time MILP scheduling model enables more efficient solving of larger subintervals (i.e. L-intervals) of the scheduling horizon compared with the corresponding discrete-time model.

Nomenclature

Sets and indices

- $\mathbf{E} = \{e\}$ Quality properties (e.g. research and motor octane number)
- $\mathbf{I} = \{i\}$ Blend components
- $\mathbf{J} = \{j\}$ Product tanks
- $\mathbf{K} = \{k\} Ll$ -periods (time periods defined for the 1st level discrete-time model)
- $\mathbf{L} = \{l\} L$ -intervals (non-overlapping subintervals of the scheduling horizon for the 3rd level continuous-time model)
- $\mathbf{M} = \{m\} L2$ -periods (time periods defined for the 2^{nd} level discrete-time model)
- $N = \{n \mid 0, 1, ..., N\}$ Time slots assigned for the entire horizon (3rd level continuous-time model)

 $\mathbf{O} = \{o\}$ – All demand orders

 $\mathbf{P} = \{p\}$ – Different products

Parameters

- *H* Length of the entire scheduling horizon
- $Q_{bc,L1}(i,e,k)$ Quality *e* of blend component *i* during *L1*-period *k*
- $Q_{pr}^{\min}(p,e)$, $Q_{pr}^{\max}(p,e)$ Minimum and maximum specifications for quality property *e* and product *p*

Continuous variables

- $Q_{pr,L1}(p,e,k)$ Quality *e* of product *p* during L1-period *k*
- r(i, p, k) Continuous variable at the 1st level, but a parameter at the 2nd and 3rd levels. Blend recipe for product *p* in *L1*-period *k*
- $V_{blend,L1}(p,k)$ Volume blended of product p during L1-period k
- $V_{comp,L1}(i, p, k)$ Volume of component *i* used in product *p* during *L1*-period *k*
- $BlendCost_{L1}$ Cost of the materials used in the blend (1st level solution)
- BlendCost_{1,2} Cost of the materials used in the blend $(2^{nd}$ level solution)
- $BlendCost_{L3}$ Cost of the materials used in the blend (3rd level solution)
- $SlackCost_{L1}$ Penalty for the non-zero slack variables (1st level solution)
- $SlackCost_{L2}$ Penalty for the non-zero slack variables $(2^{nd} \text{ level solution})$
- $SlackCost_{L^3}$ Penalty for the non-zero slack variables (3rd level solution)
- SwitchingCost_{L2} Cost associated with the switching operations (2nd level solution)
- SwitchingCost_{L3} Cost associated with the switching operations (3rd level solution)
- SwitchBlenderCost_{L2} Cost associated with the blend runs (2^{nd} level solution)
- SwitchBlenderCost_{L3} Cost associated with the blend runs $(3^{rd}$ level solution)
- SwitchDeliverCost_{L2} Penalty associated with delivering the same order from different tanks (2nd level solution)
- SwitchDeliverCost_{L3} Penalty associated with delivering the same order from different tanks (3rd level solution)
- SwitchTankCost_{1.2} Penalty associated with product changeovers in the swing tanks (2nd level solution)
- BlendRateVariations Term to minimize in order to reduce variations in the blending rate of a blend run
- VolumeDifference_{L3}(bl,n) Volume difference in blender *bl* during slot *n* between the virtual blend run using the average blending rate and the actual blend run
- AvgBlendRate(bl,n) Average blending rate of a blend run in blender *bl* during slot *n*
- BlendLength_{L3}(bl,n) Duration of the blend in blender *bl* during slot *n*
- VolumeBlended_{L3}(bl,n) Actual volume blended in blender *bl* in slot *n*

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Kinetics and Mass Transfer in the Hydrogenation of 2-((1-benzyl-1,2,3,6-tetrahydropyridin-4-yl)methylene)-5,6-dimethoxy--2,3-dihydroinden-1-one hydrochloride over Pt/C Catalyst

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The liquid phase hydrogenation of 2-((1-benzyl-1,2,3,6-tetrahydropyridin-4-yl) methylene)-5,6-dimethoxy-2,3-dihydroinden-1-one hydrochloride (1) over a 5 % Pt/C industrial catalyst was studied experimentally in a batch slurry reactor using methanol as a solvent. The catalyst was characterized by the adsorption techniques for specific surface area and pore volume, and by XRD for crystallinity. To investigate the intrinsic kinetics of the reaction, the effect of temperature, catalyst loading, hydrogen partial pressure and (1) concentration on the initial rate of hydrogenation was studied. The analysis of initial rate data showed that the gas-liquid, liquid-solid, and intraparticle mass-transfer resistances were not significant. The reaction scheme of (1) hydrogenation was proposed for the kinetic modelling. Apparent rate constants for all hydrogenation steps were calculated using a first order kinetic approach resulting in good agreement between the experimentally obtained and predicted concentrations. From the temperature dependence of rate constants, the activation energies of various reaction steps were calculated. The averaged activation energy of these steps was found to be 31.1 kJ mol⁻¹.

Key words:

catalyst, hydrogenation, diffusion, kinetic modelling

Introduction

Selective catalytic hydrogenation of double and triple carbon-carbon bonds is one of the fundamental reactions for the synthesis of fine and industrial chemicals. This important area of catalytic chemistry has been the foundation for the development of numerous diverse, small- and large-scale commercial hydrogenation processes, which include synthesis of fine and specialty chemicals such as agrochemicals^{1,2}, flavours and fragrances^{3–8}, food additives^{9–16} and pharmaceuticals^{17–21}.

The hydrogenation of 2-((1-benzyl-1,2,3,6-tetrahydropyridin-4-yl)methylene)-5,6-dimethoxy-2,3--dihydroinden-1-one hydrochloride (1) to 2-((1-benzylpiperidin-4-yl)methyl)-5,6-dimethoxy-2,3-dihydroinden-1-one hydrochloride (4), which is the last production step for the preparation of (4), is one such industrial important reaction. The reaction product is applied in the treatment of all kinds of senile dementia. In particular, it is useful for prevention and treatment of Alzheimer's disease by virtue of its acetyl cholinesterase inhibitory action²².

There are many processes described mainly in patent literature²³⁻³² for producing (4) and its phar-

maceutically acceptable salts. Complete chemo-selectivity is unlikely, because the starting compound (1) has more than one functionality susceptible to hydrogenation. There is a certain number of impurities that can be generated as side products of the reaction. The type of catalyst as well as reaction conditions for hydrogenation of (1) can significantly influence the yield of (4) and impurity profile. The yield of (4) can be low due to incomplete conversion of (1). Alternatively, if (1) is completely consumed, the yield of (4) can be low due to competing side reactions where a number of by-products are generated, such as 5,6-dimethoxy-2-(piperidin-4-ylmethyl)-2,3-dihydroinden-1-one hydrochloride,1-benzyl-4-((5,6-dimethoxy-2,3-dihydro-1H-inden-2-yl)methyl)-piperidine hydrochloride, 2-((1-benzylpiperidin-4-yl)methyl)-5,6-dimethoxy-2,3-dihydro-1H-inden-1-ol hydrochloride and others. Recently, the authors presented a detailed study of the search for a catalyst that would meet requirements for high reaction selectivity and at the same time high activity, good stability, and possibility of the catalyst's reuse³³. As expected in the hydrogenation of poly-unsaturated compound, different intermediates occur during the reaction. Based on experimental data, the reaction network given in Fig. 1 was derived for the hydrogenation of (1) to (4). The re-

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Fig. 1 – Reaction network for (1) hydrogenation over Pt/C catalyst

action pathway, involves the formation of (4) (with selectivity nearly 94 %), two intermediates (2,3) and two impurities (A, B) as the result of further hydrogenation of product (4)^{33,34}.

Liquid-phase hydrogenation over heterogeneous catalyst, in pharmaceutical production, is often performed in (semi)batch reactors, as they offer the possibility of a fast change of the production task, which is needed in this type of industry with production programs of a wide range of chemicals. Therefore, hydrogenation of (1) over 5 % Pt/C catalyst is carried out in mechanically agitated slurry reactors in which gas-liquid, liquid-solid and intraparticle diffusion resistances are likely to exist. For the purpose of kinetic study, it is important to ensure that the rate data are obtained under kinetically controlled regime or that the contribution of mass transfer is suitably incorporated or unimportant, under the reaction conditions studied, thereby ensuring a kinetically controlled regime. Considering the industrial significance of multiphase hydrogenation of (1) to (4) a detailed investigation on catalysis and kinetic modelling was undertaken in this work.

Experimental section

Materials

Compound (1) was produced by patent application WO/2007/015052 A1. The structure was confirmed by mass spectrum m/e 376 (M+, H⁺); and by H¹ NMR (CF₃COOD, 600MHz) analysis: δ 3.30 (m, 1H), 3.55 (m, 1H), 3.70 (m, 1H), 4.20-4.36 (m, 2H), 4.30 (s, 2H), 4.33 (s, 3H), 4.39 (s, 3H), 4.49 (m, 1H), 4.81 (m, 1H), 6.69 (s, 1H), 7.46 (s, 1H), 7.76 (s, 1H), 7.78-7.87 (m, 5H), 7.90 (s, 1H).

Commercial 5 % Pt/C catalyst (BASF, Italy) was used in hydrogenation experiments as received.

Catalyst characterisation

Textural characterisation of the catalyst samples was performed by means of nitrogen adsorption isotherms at 77 K using a Gemini 2380 Surface Area Analyzer (Micromeritics). Samples were outgassed at 423 K for 1 hour to remove adsorbed contaminants prior to the measurement. The BET specific surface area was calculated using the multipoint BET method on five points of the adsorption isotherm near monolayer coverage³⁵.

Crystalline structure of 5 % Pt/C catalyst was checked by X-ray diffraction analysis. XRD patterns were obtained with Philips PW 1830 diffractometer using Ni-filtered CuK α radiation operating at 40 kV and 30 mA. The patterns were recorded over $15^{\circ} < 2\theta < 70^{\circ}$ range using a step size of 0.02°.

Reaction procedure

The kinetic experiments were carried out in a commercial lab-scale 300 cm³ stainless steel autoclave (*Parr Instrument Company, U.S.A.*). The reactor was provided with the automatic temperature control arrangement for sampling of liquids and variable agitation speeds. The details of the reactor set up were the same as described in our earlier paper³³. In a typical hydrogenation experiment, predetermined quantities of (1), catalyst and solvent methanol were charged into autoclave. The reactor was closed and the contents flushed three times with hydrogen. The reactor was then heated up to a desired temperature, pressurized with hydrogen to a desired level, and the reaction mixture was stirred with desired agitation speed. Pressure was maintained constant throughout the course of the reaction by supplying hydrogen from a reservoir vessel through a constant pressure-regulator valve. The moment when the desired pressure was achieved was assumed as the start (time = 0) of the reaction. The samples of reaction mixture were taken periodically from reactor, diluted with methanol and analyzed using high-pressure liquid chromatography. In the reaction mixture, the concentration of reactant (1), product (4), two intermediates (2, 3) and two impurities (A, B) were monitored. The ranges of operating conditions are given in Table 1.

Table 1 - Range of parameters

Catalyst loading, g dm ⁻³	0.57 - 2.86
Stirring speed, min ⁻¹	100 - 500
H ₂ partial pressure, MPa	0.2 - 3.0
(1) concentration, mol dm^{-3}	73 – 243
Temperature, K	298 - 318

Scale up of hydrogenation reaction on the industrial scale was conducted in *Pfaudler* batch reactor, $V = 630 \text{ dm}^3$ (*Pfaudler*). The reactor was made of steel and equipped with a gas supply system (hydrogen and nitrogen). The reactor was heated by the reactor jacket and equipped with a sampling system.

The analysis of all samples was carried out using Agilent Technologies high-pressure liquid chromatography (model 1200) with DAD detector. The analytical conditions were as follows: Column & Packing: Phenomenex Gemini C18, 250 x 4.6 mm (5 μ m); Eluent A: Buffer NH₄OAc 10 mmol L⁻¹, pH = 6 diluted with acetonitrile in ratio of 2.7:1; Eluent B: Buffer NH₄OAc 10 mmol L⁻¹, pH = 4 diluted with acetonitrile in ratio of 0.54:1 Gradient: 0. min – 100 % A, 20. min – 0 % A Equilibration time: 20 min; Injection volume: 20 μ L; Flow rate: 2.0 cm min⁻¹; Wavelength: 277 nm; Column temperature: 308 K; Autosampler temperature: 293 K. NMR analysis was recorded on Bruker Avance DRX 600 NMR spectrometer operating at 600.1 and 150.9 MHz. CF₃COOD was used as a solvent.

Results and discussion

Catalyst characterization

The BET surface area and total pore volume of the supported Pt catalyst were 761 m² g⁻¹ and 0.39 cm³ g⁻¹, respectively. In addition, the mean diameter of pores obtained from BET plot and pore size distribution was 2.04 nm.

The XRD pattern of Pt/C catalysts was collected in the range from 15° up to 70°. The catalyst exhibits a typical face-centred cubic (FCC) pattern, with the diffraction peaks at ~ 39°, 46° and 67°, assigned to the corresponding (111), (200) and (220), respectively (Figure 2). Several graphitic reflections are evident, the strongest of which is a sharp, symmetrical peak at $2\theta = 26.3^{\circ}$ assigned as the [002] plane of graphite^{35,36}. The broad peaks in the XRD patterns indicate the small sizes of nanocrystals. The mean crystallite size derived from (220) plane XRD peak broadening, by applying the Scherrer's equation, was 7.6 nm.



Fig. 2 – X-ray diffraction pattern of 5 % Pt/C catalyst

Kinetic studies

The hydrogenation experiments using 5 % Pt/C catalyst were performed to understand the overall kinetic of this reaction. For this purpose, experimental data were obtained by varying the operative conditions to observe the initial rate of hydrogenation as well as the integral concentration-time profiles. According to GLC and NMR data, the reaction pathway, as presented in Fig. 1, involves the formation of (4) (with selectivity nearly 94 %), two intermediates (2, 3) and two impurities (A, B) as a result of further hydrogenation of product (4). Impurity (B) is most difficult to eliminate by crystallization and re-crystallization processes³³. At the end

of reaction, its content in the reaction mixture should not exceed $2.8 \cdot 10^{-4}$ mol dm⁻³. Also, the content of impurity (A) should be below $1.0 \cdot 10^{-3}$ mol dm⁻³. Since the formation of impurities A and B were below these values in all experiments, the reaction scheme presented in Fig. 1 was simplified as shown in Fig. 3.



Fig. 3 – Simplified reaction scheme for (1) hydrogenation over Pt/C catalyst

The typical kinetic curves are presented in Fig. 4, demonstrating the dependence of the products composition *versus* reaction time at hydrogen pressure $p_{\rm H2} = 0.2$ MPa and temperature 308 K over 5 % Pt/C catalyst.



Fig. 4 – Comparison of the model prediction (solid lines) with experimental data (symbols) of (1) hydrogenation over 5 % Pt/C ($c_1 = 0.14 \text{ mol } dm^{-3}$; $p_{H2} = 0.2 \text{ MPa}$; T = 318 K; $m_{cat} = 1.71 \text{ g } dm^{-3}$; $V_{MeOH} = 0.175 \text{ dm}^3$, $N = 400 \text{ min}^{-1}$)

Analysis of initial hydrogenation rates

The first approach to understanding the dependency of reaction rates on the individual reaction parameters as well as the significance of the mass transfer effect is the analysis of initial rate data. The separate effect of initial concentration of (1), hydrogen pressure and temperature on the initial rate data of hydrogenation of (1) was studied and the results are presented in Figs. 5-8.

The effect of concentration of (1), on the initial rate of hydrogenation is shown in Fig. 5. The rate of (1) hydrogenation is first order in the substrate at low concentration of substrate and approaches zero



Fig. 5 – Effect of (1) concentration on initial rate of hydrogenation ($p_{H2} = 0.2 \text{ MPa}$; $m_{cat} = 1.71 \text{ g } dm^3$; T = 308 K; $V_{MeOH} = 0.175 \text{ dm}^3$, $N = 400 \text{ min}^{-1}$)

order at high concentrations of the substrate. These results indicate the non-linear behaviour of the rate of (1) hydrogenation, which is characteristic of a surface controlled reaction.

The initial reaction rates were also determined at various hydrogen pressures. Fig. 6 indicates nearly zero order dependence of the initial rate of reaction on hydrogen pressure, except at low partial pressures of hydrogen where the rate is directly proportional to the hydrogen pressure, and thus effectively exhibiting a first-order dependency on hydrogen.



Fig. 6 – Effect of hydrogen pressure on initial rate of hydrogenation ($c_1 = 0.14 \text{ mol } dm^{-3}$; $m_{cat} = 1.71 \text{ g } dm^{-3}$; T = 308 K; $V_{MeOH} = 0.175 \text{ } dm^3$, $N = 400 \text{ min}^{-1}$)

The effect of temperature on the initial hydrogenation rate was studied in the range from 298 up to 318 K, at constant hydrogen pressure (0.2 MPa), and the results are presented in Fig. 7.



Fig. 7 – Effect of temperature on initial reaction rate ($c_1 = 0.14 \text{ mol } dm^3$, $V_{MeOH} = 0.175 \text{ } dm^3$, $p_{H2} = 0.2 \text{ } MPa$, $m_{cat} = 1.71 \text{ } g \text{ } dm^3$, $N = 400 \text{ min}^{-1}$)

As can be seen, the initial reaction rate varied linearly with temperature, which suggested that the reaction was intrinsically kinetically controlled and the activation energy values should be determined.

Influence of mass transfer

For the purpose of kinetic study, it is important to ensure that the rate data obtained were under conditions of chemical reaction control and that these data were not significantly influenced by mass transfer limitation. The initial rate data were analysed to check the significance of external (gas-liquid and liquid-solid) and internal mass transfer resistance.

The rate of reaction in a multiphase reactor for the case of first order reaction is given by the following equation proposed by Satterfield and Sherwood³⁷,

$$\frac{c_{\rm A}^*}{r_{\rm A}} = \frac{1}{k_{\rm gl}a_{\rm g}} + \frac{1}{m} \left[\frac{1}{k_{\rm ls}a_{\rm s}} + \frac{1}{k \, a_{\rm s} \eta} \right]$$
(1)

A plot of the inverse of the rate of reaction *versus* the inverse of catalyst mass density should give a straight line. This plot is given in Fig. 8 for experiments where the catalyst mass was varied from 0.57 to 2.86 g dm⁻³.

The term $1/k_{1s}a_s$ of the plots in Fig. 8 represents a resistance associated with transport of hydrogen through bulk liquid. The term $1/k a_s \eta$ represents a resistance associated with the surface reaction. The intercept $1/k_{g1}a_g$ represents a resistance to gas adsorption across gas-liquid interface. From the intercept $k_{g1}a_g$ was 0.79 min⁻¹.

Further, in order to analyse the contribution of liquid-solid and intraparticle mass transfer effects on the rate of (1) hydrogenation, a knowledge of the liquid-solid mass transfer coefficient, k_{s} , effective



Fig. 8 – Effect of inverse catalyst loading on the inverse of the rate of (1) hydrogenation ($c_1 = 0.14 \text{ mol } dm^3$, $p_{H2} = 0.2 \text{ MPa}$, T = 308 K, $V_{MeOH} = 0.175 \text{ } dm^3$, $N = 400 \text{ min}^{-1}$)

diffusivity, D_{e} , external surface area of the catalyst particle, a_{s} , saturation solubility, c_{A}^{*} and the overall rate of hydrogenation, r_{A} are required.

The external surface area of the catalyst particle was calculated from the following equality, $a_s = m(6/d_p)(\rho_1/\rho_s)$ and was $260 \text{ m}_{cat}^2 \text{ m}_1^{-3}$. Solubility of hydrogen in methanol have been reported by Choudhary *et al.*³⁸ for relevant pressures and temperatures (293–328 K and 2.13 – 0.48 MPa) and a value of $H = 4.2 \cdot 10^{-2}$ MPa m³ mol⁻¹ was predicted from these data.

The effective diffusion coefficient, D_{e} is obtained from the molecular diffusion coefficient, D the catalyst particle porosity, e and tortuosity, t from the following expression

$$D_{\rm e} = D \frac{\varepsilon}{\tau} \tag{2}$$

The tortuosity and porosity of the catalyst were assumed to be 4 and 0.5, respectively³⁹.

The molecular diffusion coefficient for component dissolved in a solvent is calculated from Wilke and Chang⁴⁰ equation

$$D = 7.4 \cdot 10^{-12} \frac{T \sqrt{\chi M}}{\mu_1 v^{0.6}}$$
(3)

The calculated value of effective diffusivity along with other parameters is shown in Table 2.

The Weisz-Prater criterion^{41,42} was used to determine diffusion resistance in porous Pt/C catalyst

$$\phi = \frac{r_{\rm A}(d_{\rm p}/2)^2}{c_{\rm A,s}D_{\rm e}}$$
(4)

From Equation (4) using parameters given in Table 2, a value of Thiele modulus ϕ was calculated. A value for $\phi = 6.6 \cdot 10^{-4}$ indicates that the surface reaction rate is lower than the diffusion rate of a reactant within the pores of a catalyst⁴² and the effectiveness factor ($\eta = \text{tgh}\phi/\phi$) was 0.99.

Table	2 –	Values of different parameters used in evaluating
		the role of external and internal mass transfer re-
		sistance

Catalyst/reactor data				
Catalyst particle diameter	$d_{\rm p} = 2.5 \cdot 10^{-5} {\rm m}$			
Catalyst particle density	$ ho_{\rm s}$ = 1500 kg m ⁻³			
Tortuosity factor	au=4			
Particle porosity	$\varepsilon = 0.5$			
Catalyst loading	$m = 1.75 \text{ kg m}^{-3}$			
Solvent	methanol			
Liquid density	$\rho_1 = 791.8 \text{ kg m}^{-3}$			
Liquid viscosity	$\mu_1 = 5.9 \cdot 10^{-3} \text{ kg m}^{-1} \text{ min}^{-1}$			
Stirring speed	$N = 400 \text{ min}^{-1}$			
Reactor volume	$V_{\rm R} = 3 \cdot 10^{-4} {\rm m}^3$			
Reaction condit	ions/parameters			
Reaction temperature	<i>T</i> =308 K			
H_2 pressure (constant)	$p_{_{\rm H2}} = 0.2 { m MPa}$			
Initial (1) concentration	$c_1 = 1.4 \cdot 10^2 \text{ mol m}^{-3}$			
Henry coefficient	$H = 4.2 \cdot 10^{-2} \text{ MPa m}^3 \text{ mol}^{-1}$			
Effective diffusion coefficient	$D_{\rm e} = 2.4 \cdot 10^{-8} {\rm m}^2 {\rm min}^{-1}$			

The value of rate constant, k was calculated using equation (5)

$$r_{\rm A} = k \eta \, a_{\rm s} \frac{p_{\rm H_2}}{H} \tag{5}$$

and it was $1.63 \cdot 10^{-3} \text{ min}^{-1}$, at hydrogen pressure of 0.2 MPa. From the slope of the curve presented in Fig. 5 and calculated values for k, a_s and η , the liquid-solid resistance was determined as $k_{1s}a_s = 0.137 \text{ min}^{-1}$.

This analysis provides a rough indication that the external and internal mass-transfer resistances do not affect the rate of (1) hydrogenation i.e. hydrogenation rate is kinetically controlled. This conclusion was confirmed by the values of external effectiveness factors (gas-liquid) η_{gl} and (liquid-solid) η_{ls} which were 0.999 and 0.997 respectively.

Estimation of kinetics parameters

In order to describe the concentration profile of the species participating in the hydrogenation of (1), the simple estimating reaction scheme was proposed (Figure 3). According to the reaction scheme, first order kinetics with respect to the organic compounds was assumed for all hydrogenation steps

$$r_{\rm i} = k c_{\rm H_2} c_i = k^{\rm c} c_i \tag{6}$$

where the product $k c_{\rm H2}$ was lumped pseudo-first order constant, because the hydrogen pressure in the gas phase was maintained constant in all experiments ($p_{\rm H_2} = 0.2$ MPa), and because the solubility of hydrogen in the liquid phase was determined by its solubility in the solvent (as the concentration of substrate was low compared to the solvent concentration). The first order kinetic approach essentially assumes non-significant coverage of adsorbed reactant, which was justified by utilization of low (1) concentration.

The reaction kinetics can be described as follows. The disappearance of the reactant and the generation of the products can be calculated by the solution of the molar balances for the components in a batch reactor:

disappearance of reactant (1)

$$r_1 = -\left[\left(k_1 + k_2\right)c_1\right] \tag{7}$$

generation of intermediate (2)

$$r_2 = k_1 c_1 - k_3 c_2 \tag{8}$$

generation of intermediate (3)

$$r_3 = k_2 c_1 - k_4 c_2 \tag{9}$$

generation of product (4)

$$r_4 = k_3 c_2 + k_4 c_3 \tag{10}$$

The apparent rate constant was determined based on the simple kinetic models. The model parameters were estimated by minimising the objective function

$$RMSD = \sum_{k=1}^{k=4} \frac{1}{N} \sqrt{\sum_{i=1}^{i=N} \left[\left(\frac{c_{k(\text{mod}),i} - c_{k(\text{exp}),i}}{c_{k,\text{max}}} \right)^2 \right]} \quad (11)$$

where $c_{k(\text{mod}),i}$ is the calculated concentration of component *i*, $c_{k(\text{exp}),i}$ is measured concentration of component *i*, *n* is number of samples, and *k* is number of independent measured variables. The rate parameters estimated and *RMSD* values are given in Table 3 when hydrogenation of (1) was performed at various temperatures.

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	(1)				
<i>T</i> , K	k_{1}	k_2	<i>k</i> ₃	k_4	RMSD
298	0.00194	0.00952	0.00556	0.01163	0.00626
303	0.00213	0.01540	0.00714	0.01423	0.00561
308	0.00241	0.01974	0.01004	0.02102	0.00618
318	0.00318	0.02466	0.01605	0.02831	0.00648

Table 3 – Estimated kinetic parameters for hydrogenation of

Example of the fit is provided in Figures 4 and 9 (when the reaction was carried out in laboratory and industrial reactor) showing apparently good agreement between the experimentally measured and predicted concentrations. The experimental and the predicted concentration-time data were found to agree within 5–9 % error.



Fig. 9 – Comparison of the model prediction (solid lines) with experimental data (symbols) of (1) hydrogenation over 5 % Pt/C in industrial reactor ($c_1 = 0.14 \text{ mol } dm^{-3}$, $p_{H2} = 0.2 \text{ MPa}$, T = 308 K, $m_{cat} = 1.71 \text{ g } dm^{-3}$, $N = 400 \text{ min}^{-1}$, $V_R = 40 \text{ dm}^3$)

The first order kinetic model allows estimation of the rate constants in (1) hydrogenation with high accuracy despite the apparent simplicity. The first order kinetic model is valid in the case of low surface coverage only and neglects differences in adsorption.

The observed energies of activation for formation of intermediates and product of reaction were determined from the Arrhenius plot shown in Fig. 10, in which the rate constants against the reciprocal of the temperature were plotted. The experiments were carried out in the temperature range 298 – 318 K at constant hydrogen pressure (0.2 MPa). From the temperature dependence of rate parameters, the activation energies of various reaction steps were calculated. These values of activation energies for steps, r_1 , r_2 , r_3 and r_4 are presented in Table 4.



Fig. 10 – Temperature dependence of rate constants

Table 4 – Activation energies for steps r_{μ} , r_{ν} , r_{s} and r_{4}

	Reaction	$E_{\rm a}$, kJ mol ⁻¹
r_1	$A \rightarrow B$	40.8
r_2	$B \rightarrow R$	34.3
<i>r</i> ₃	$A \rightarrow C$	14.4
r_4	$C \rightarrow R$	34.7

Hydrogenation of reactant (1) to intermediate (3) (A \rightarrow B) is rate determining step deducing from high value for energies of activation, E_a . The hydrogenation of C=C double bond in the bridge of reactant (1) molecule is very quick (A \rightarrow C) with low value for E_a . Energies of activation for hydrogenation of both intermediates (2) and (3) to product (4) (B \rightarrow R, C \rightarrow R) are practically the same. The value of the averaged activation energy of these four reaction steps, 31.1 kJ mol⁻¹, is in agreement with those generally reported for the double bond hydrogenation reaction carried out in kinetic regime^{18, 43-46}.

Conclusion

The hydrogenation of 2-((1-benzyl-1,2,3,6-tetrahydropyridin-4-yl)methylene)-5,6-dimethoxy-2,3dihydroinden-1-one hydrochloride (1) to 2-((1-benzylpiperidin-4-yl)methyl)-5,6-dimethoxy-2,3-dihydroinden-1-one hydrochloride (4) using a 5 % Pt/C catalyst was studied in a batch slurry reactor in a temperature range of 298 - 318 K using methanol as solvent. The influence of catalyst loading, hydrogen partial pressure, and reactant concentration on the hydrogenation rate was investigated. The analysis of initial rate data showed that the gas-liquid, liquid-solid, and intraparticle mass-transfer resistances were not significant. The reaction scheme of (1) hydrogenation was proposed for the kinetic modelling. Apparent rate constants of all hydrogenation steps were estimated by the first-order kinetic approach. Very good agreement between experimentally recorded concentrations and those predicted by the kinetic model was achieved. From the temperature dependence of rate constants, the activation energies of various reaction steps were calculated. The averaged activation energy of these steps, 31.1 kJ mol⁻¹ is in agreement with that generally reported for the double bond hydrogenation reaction carried out in kinetic regime.

Nomenclature

- \vec{c}_{A} saturation solubility of H₂, mol m⁻³
- c_{As} surface concentration of A, mol m⁻³
- c_1 concentration of reactant (1), mol m⁻³
- c_2 concentration of intermediate (2), mol m⁻³
- c_3 concentration of intermediate (3), mol m⁻³
- c_4 concentration of product (4), mol m⁻³
- d_{p} catalyst particle diameter, m
- D molecular diffusion coefficient, m² min⁻¹
- D_{e} effective diffusion coefficient, m² min⁻¹
- E_{a} activation energy, kJ mol⁻¹
- H Henry coefficient, MPa m³ mol⁻¹
- $k_1 k_4$ reaction rate constant of respective steps, min⁻¹
- $k_{gl} a_g$ gas-liquid mass transfer coefficient, min⁻¹
- $k_{1s} a_{s}$ liquid-solid mass transfer coefficient, min⁻¹
- m catalyst loading, kg m⁻³
- M molecular mass, kg mol⁻¹
- N stirring speed, min⁻¹
- $p_{_{\rm H_{2}}}$ hydrogen pressure, MPa
- $r_1 r_4$ reaction rate of respective steps, mol m⁻³ min⁻¹
- t time, minutes
- T temperature, K
- v molar volume, mol m⁻³

Greek letters

- χ association factor of solvent,–
- ε particle porosity, –
- ϕ Thiele modulus, –
- η effectiveness factor, –
- μ_1 liquid dynamic viscosity, kg m⁻¹ min⁻¹
- ρ_1 liquid density, kg m⁻³
- τ tortuosity factor, –

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