Effects of Raschig Ring Packing Patterns on Pressure Drop, Heat Transfer, Methane Conversion, and Coke Deposition on a Semi-pilot-scale Packed Bed Reformer

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The effects of Raschig ring packing patterns on the efficiency of dry methane reforming reactions were investigated using computational fluid dynamics (CFD). The present study aims to understand the behavior of fluid flow in packed bed reactors, especially under low reactor-to-ring ratios between 4 and 8. Three packing patterns were studied: vertical staggered (VS), chessboard staggered (CS), and reciprocal staggered (RS). It was determined that packing pattern notably affected pressure drop across the reactor length. The VS pattern produced the lowest pressure drop of 223 mPa, while the CS and RS patterns produced pressure drops of 228 mPa and 308 mPa, respectively. The values of methane conversion can be increased by ca. 2 % by selecting a more suitable packing pattern (i.e., 76 % for the VS pattern and 74 % for the CS and RS patterns).

Kevwords:

packed bed reactor, Raschig ring, dry methane reforming, reactions kinetics

Introduction

Due to the global issue of elevated greenhouse gas emissions, the search for alternative low pollution energy sources remains necessary. Notably, the use of synthesis gas represents an option for decreasing greenhouse gas from industries, since methane (CH_4) and carbon dioxide (CO_2) are commonly employed as reactant gases for synthesis gas production. Moreover, synthesis gas can be used as raw material for the synthesis of Fischer-Tropsch synthesis, methanol, ammonia, and dimethyl ether (DME)¹⁻⁴. Typically, the reaction equilibrium to produce syngas is:

> $CH_4 + CO_2 \xrightarrow{Catalyst} 2CO + 2H_2$ (1)

Nevertheless, the thermodynamic barrier represents a major challenge and is unfavorable to processes that rely merely on heat to convert the two-carbon molecules of methane and carbon dioxide at high conversion levels⁵. The key to the success of the dry reforming process depends on the management of heat distribution for this highly endothermic reaction process. The use of catalyst systems may lead to a reduction in energy invested in the process, which would allow dry reforming to become closer to an economical process downstream. Metal catalysts are suitable for reforming processes. Using nickel-based catalysts-either directly or supported–is one of the most commonly reported methods^{5–12}. Furthermore, it has been reported that many nickel-based catalysts are efficient in inducing dry methane reforming (DMR) at lower temperatures than predicted based on equilibrium calculations.

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Due to DMR being confined from two moles of methane and carbon dioxide to four moles of products, this reaction favors low pressure. Advanced catalyst shapes have been presented for higher catalyst activity at a lower pressure drop across the bed. The reformer throughput at a fixed operating temperature, pressure, and inlet gas composition largely relies on the activity of the unit of volume of the catalyst bed. Fukuhara et al. also worked with a nickel-based catalyst impregnated on honeycomb-like structure. They reported that this catalyst was more efficient at high temperature (700 °C) and exhibited less deactivation¹³. Moreover, utilizing a wall-coated catalyst is an alternative technique that possibly prevents the coke formation that can occur inside the packed column due to hotspot problems; however, metal oxide catalysts have proven to be less sensitive to carbon deposition on the catalyst surface¹⁴. Notably, the application of a wall-coated catalyst is known to improve heat and mass transfer. A typical DMR process is performed in packed bed reactor that must supply heat to this highly endothermic reaction.

The modified packed bed reactor is a promising technology that is a fundamental ideal for chemical reactions with low energy consumption, minimum contamination, and the ability to control the non-ideal behavior of gas mixtures inside a packed bed reactor. At the industrial level, a packed bed reactor is widely used in chemical and petrochemical processes, such as methanol synthesis, ammonium synthesis, and Fischer-Tropsch synthesis¹⁻⁴. Typically, reactors consist of the reaction zone (or effective volume), where reactant(s) flow and contact with catalytic packing to transform into product(s). The design of a packed bed is based on the mechanisms of fluid flow, heat transfer, and internal mass transfer limitations¹⁵. Moreover, particle shape will impact pressure drop, while the complex structural system in a randomly packed bed typically results in flow and temperature maldistributions. At high tube-to-particle diameter ratios (N), generally between 50 and 500, which represents the average amount of catalyst particles on a cross-section of the diameter, the wall effects can be negligible since the affected area is very small compared to the reactor bulk. Optimization of the tube-to-particle ratio strategy has attracted many reseachers¹⁶⁻¹⁹. In extremely exo- and endothermic processes, the heat flowing axially through the bed is one of the most important factors. The challenge is to increase the heat transfer rate from the reactor wall to the packed bed. For example, a low tube-to-particle ratio (N =4-8) was investigated on large void fractions existing in the near-wall region^{5,20,21}. Furthermore, stagnation or backflow can be observed in the wake of the particles, with high velocities being detected in

regions with high void fractions²¹. Uncontrolled heat transfer may lead to undesired products, selectivity, and yields, sometimes resulting in reactor damage.

Recently, computational fluid dynamics (CFD) has been used to simulate the flow and heat transfer characteristics of packed beds at low aspect ratios. For example, Nijemeisland and Dixon²⁰ studied a packed bed of spheres with a low tube-to-particle diameter ratio of 2. The pressure profile within the bed was investigated using CFD. The authors determined that, using a sphere diameter of 99 % of the actual sphere diameter, had led to a turbulent solution while maintaining the original velocity distribution around the contact points. Further studies have been conducted on fluid flow, heat transfer, and dispersion in either low-*N* packed tubes or small periodic groups of spherical particles without reaction.

In cases using randomly filled tubular fixed bed reactors with small tube-to-particle diameter ratios, the lattice Boltzmann approach can provide detailed insight into flow and transport processes in complex geometries²¹. However, the inclusion of chemical reactions been limited to lattice Boltzmann simulations of isothermal flows with surface reactions to date, have shown strong agreement among computational and experimental results^{22–24}.

Although a randomly packed bed is more commonly used due to the ease of packing and acceptable pressure drop values, Nijemeisland and Dixon studied a random catalyst packed bed using numerical techniques and experiments to reflect the local effects²⁰. Moreover, Dixon et al. determined DMR endothermic reactions by coupling fluid flow in the packed bed to transport and react inside catalyst particles using CFD²⁵. The authors observed that temperature, concentration, and reaction rate at catalyst particles are heterogeneous near the wall. Additionally, Nijemeisland et al.26 also used CFD to compare catalyst geometries and hole sizes for non-reactive heat transfers. The modelling of low tube-to-particle ratio beds that are used in extremely exo- and endothermic processes in shell-and-tube type reactors is complicated due to the presence of radial temperature profiles across the tube²⁷. Therefore, the physical mechanisms involved, especially in the wall vicinity, must be understood in order to develop a non-intrusive tool to collect numerical data for comparison against experimental results. Packing technology ideas are used to design fluid flow in a packed bed by determining patterns that minimize maldistribution and pressure drops in a low tube-to-particle ratio. The present study compares simulation results with experimental results to determine the validity of the kinetic model.

The goal of the present study was to present three practicable Raschig ring packing patterns— VS, CS, and RS. The present study used a semi-pilot scale reformer reactor 10.16 cm in diameter and 5.16 cm in length. A low tube-to-particle ratio (N)(4–8) was used to provide information concerning the limitations of heat and mass transfer, catalyst deactivation, and system controllability. Several experiments were performed to determine the overall reaction conversion. Due to being a semi-pilot-scale project, the CFD models were constructed to illustrate the velocity, temperature, pressure, and concentration profiles inside a reactor. In this work, kinetic parameters were validated using a lab-scale packed bed filled with 10 % Ni/Al₂O₂-MgO coated on Raschig ring structures. The effect of various influencing parameters, such as feed velocity and feed concentration parameters, were used in the CFD models in order to reflect the catalytic performance via computational analysis. Finally, the experimental results and the CFD approach were used to clarify the holistic effects of the three packing patterns on a studied reformer.

Materials and methods

In the present study, the experimental rig was fabricated to conduct the DMR reaction in a laboratory-scale packed bed reactor (5 catalyst pellets) and a semi-pilot-scale packed bed reactor (20–24 catalyst pellets). The experimental program was divided into two parts, i.e., study of the kinetic parameters in a laboratory-scale packed bed reactor, and effects of packing patterns in a semi-pilot-scale packed bed reactor.

Catalyst preparation

Sol-gel procedure

Raschig rings coated with 10 % Ni/Al₂O₂-MgO catalyst were prepared using the sol-gel method. In brief, the sol-gel synthesis of the catalyst required aluminum isopropoxide $(Al(OC_{3}H_{7})_{3})$, nickel(II) nitrate $(Ni(NO_3)_2) \cdot 6H_2O_3$, and magnesium ethoxide 98 % (Sigma-Aldrich®, Thailand) (Mg(OC,H₅)) as precursors. The aluminum isopropoxide was dissolved in water to undergo hydrolysis. It was then changed into a gel by addition of nitric acid. The magnesium ethoxide precursor was dissolved separately in water, and then added into the gel. The precursors were refluxed for ca. 12 h. The Ni solution was added to the sol-gel solution under vigorous stirring. The obtained solution was maintained under stirring for ca. 1 h until a green gel was formed. The technique has been described previously by Piyapaka²⁸.

Coating procedure

Raschig rings were used as the substrate for sol-gel dip coating. Firstly, the surfaces of Raschig rings were washed with deionized water (DI water) in an ultrasonic bath for cleaning and removal of impurities and organic compounds. For the Raschig ring dip coating process, the rings were arranged in a vertical direction during coating to cover the entire ring surface. They were then immersed in an ultrasonic bath of sol-gel solution for 25 min. Finally, the Raschig rings were dried and calcined in air at 450 °C by controlling the heating rate (1 °C min⁻¹), as shown in Fig. S1.

The specific surface areas of Raschig ring wall-coated catalysts were measured using a BEL-SORP-mini instrument. The samples were degassed at 350 °C for 4 h prior to N₂ physisorption. The specific surface area of 10 % Ni/Al₂O₃-MgO was 177.68 m² g⁻¹, while its pore volume was 8.92 cm³ g⁻¹ with a pore diameter of 0.201 nm.

Experimental system and procedure

Laboratory-scale setup for the study of kinetics: Optimizing the rate constants

The kinetic study of the DMR reaction was performed in a packed bed reactor (1.587 cm diameter). Five pellets of Raschig ring catalyst were used for the kinetic study, as presented in Fig. S2. The reactor was placed in an electrically heated furnace, and its temperature was controlled by an intelligent temperature control meter (Carbolite Model. VST12/600/3216P1). The inlet flow rate of reactant gases, CH_{4} and CO_{2} , was controlled by a mass flow controller (Kofloc model 8500). A schematic of the DMR system is presented in Fig. S3. Before the reaction occurred, the Raschig ring coated with 10 % Ni/Al₂O₂-MgO catalyst was reduced by flowing H_2/N_2 (40 % H₂ by volume) into the reactor with the temperature increasing from room temperature to 600 °C over 12 h. The samples were tested in a 600 - 800 °C temperature range.

A mathematical model of kinetic reaction was developed using COMSOL Multiphysics V3.5a software, which facilitated the design of geometries and boundary conditions. The simulation environment of this software facilitates all steps in the modelling process. In the present study, COMSOL Multiphysics V3.5a was used to build the numerical model describing the effect of packing pattern on the DMR reaction, and its extensive interface, excel, was used to determine the reaction rate constants of this process. The algorithm proceeds as follows. Since the reactions were assigned to occur at the catalyst surfaces, the catalyst thickness, porosity of catalyst layer, and tortuosity of fluid in the

Experimental data: $C_{i \exp}$ [mol m ⁻³]										
Run 1		Run 2		Run 3		Run 4		Run 5		Optimization of k' [s ⁻¹]
$[CH_4]_{in}$	[CH ₄] _{out}	[CH ₄] _{in}	[CH ₄] _{out}	$[CH_4]_{in}$	[CH ₄] _{out}	[CH ₄] _{in}	[CH ₄] _{out}	$[CH_4]_{in}$	[CH ₄] _{out}	
2.848	4.257	4.658	5.798	5.877	6.408	6.670	6.886	7.240	7.155	$k_1 = 0.1601$
2.848	4.211	4.658	5.734	5.877	6.338	6.670	6.810	7.240	7.077	$k_2 = 0.1638$
2.848	4.164	4.658	5.671	5.877	6.267	6.670	6.734	7.240	6.998	$k_3 = 0.1677$
2.848	4.117	4.658	5.606	5.877	6.196	6.670	6.658	7.240	6.918	$k_4 = 0.1716$
2.848	4.069	4.658	5.542	5.877	6.125	6.670	6.581	7.240	6.839	$k_5 = 0.1756$
2.848	4.022	4.658	5.477	5.877	6.053	6.670	6.581	7.240	6.759	$k_6 = 0.1797$
2.848	3.974	4.658	5.412	5.877	5.981	6.670	6.427	7.240	6.678	$k_7 = 0.1838$
2.848	3.926	4.658	5.346	5.877	5.909	6.670	6.349	7.240	6.597	$k_8 = 0.1881$
2.848	3.878	4.658	5.281	5.877	5.837	6.670	6.271	7.240	6.516	$k_9 = 0.1925$
2.848	3.829	4.658	5.215	5.877	5.764	6.670	6.193	7.240	6.435	$k_{10} = 0.1970$
2.848	3.781	4.658	5.149	5.877	5.691	6.670	6.114	7.240	6.353	$k_{11} = 0.2016$
2.848	3.732	4.658	5.082	5.877	5.617	6.670	6.035	7.240	6.271	$k_{12} = 0.2063$
2.848	3.683	4.658	5.016	5.877	5.544	6.670	5.956	7.240	6.189	$k_{13} = 0.2111$
2.848	3.634	4.658	4.949	5.877	5.470	6.670	5.877	7.240	6.107	$k_{14} = 0.2160$
2.848	3.585	4.658	4.883	5.877	5.396	6.670	5.798	7.240	6.024	$k_{15} = 0.2210$
2.848	3.536	4.658	4.816	5.877	5.322	6.670	5.718	7.240	5.942	$k_{16} = 0.2262$
2.848	3.487	4.658	4.749	5.877	5.248	6.670	5.639	7.240	5.859	$k_{17} = 0.2314$
2.848	3.438	4.658	4.681	5.877	5.174	6.670	5.559	7.240	5.776	$k_{18} = 0.2368$
2.848	3.388	4.658	4.614	5.877	5.100	6.670	5.479	7.240	5.693	$k_{19} = 0.2423$
2.848	3.339	4.658	4.547	5.877	5.025	6.670	5.399	7.240	5.610	$k_{20} = 0.2480$

Table 1 – Experimental data and the optimization of k' constants

catalyst layer were not included in the model. The concentration of species *i* or C_i , and the rate equation of species *i* or r_i were introduced in the numerical models presented in Eqs. 2 and 3.

$$\nabla \cdot (-D\nabla c_i) + u \cdot \nabla C_i - r_i = 0 \tag{2}$$

$$-r_i = k' \cdot C_i \tag{3}$$

In order to obtain the reaction rate constants k', the numerical program was performed as shown in Fig. 1. In the first step, the initial predictions of rate constants (k') and the concentration of component C_i at the Raschig ring surface must be offered for numerical model; then, the simulation can start, end, and determine the interval times. The concentrations from simulation were obtained for comparison against experimental results at each measured point. All deviations between experimental and calculated values were squared and summed to form an objective function (J) (Eq. 4). The constant k'using the least square method during the cycle were determined as the lowest sum of squared differences J of experimental and modelling components' final concentrations. The results of alternatives of k' constant are presented in Table 1.

$$J = \sum_{i=1}^{n} \left(C_{i_model} - C_{i_exp} \right)^{2}$$
(4)

After discovering the reaction rate constants, (illustrated in Fig. 2), the model was compared with experimental data. Reaction rate constants were obtained by fitting the mathematical model to experimental data generated from the Raschig ring packing pattern for the DMR reaction. It was observed that the lowest objective function J was at $k'_{11} = 0.2016$. Then, the rate constant k'_{11} was called k', which presented the rate constant that combined the catalyst characteristic parameter "a" (Eq. 8).

For the DMR reaction, the rate constant is defined as the rate of concentration of a substance involved in the reaction with a minus or plus sign attached, depending on whether the substance is a reactant or a product, respectively²⁵. The rate constant is the constant of proportionality "*k*" in the rate equation, as expressed by Eqs. 5 - 7:

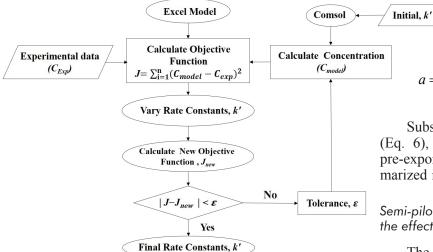


Fig. 1 – Schematic of numerical model optimization

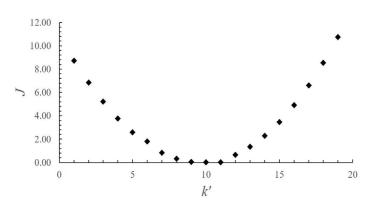


Fig. 2 – Optimization data plot of the k' constant and objective function J

Table 2 – Simulation conditions					
Parameters	Value	Unit			
E _a	$1.02 \cdot 10^{6}$	J mol ⁻¹			
$k_{_0}$	0.2016	S^{-1}			
A_{cat}	150	m^2			
W_{cat}	0.025	g			
A_{ring}	4.41 · 10 ⁻³	m^2			
V_{R}	1.1179	m ³			

$$-r_{\mathrm{CH}_4} = k' \cdot C_{\mathrm{CH}_4} \tag{5}$$

$$-R_{\rm CH_4} = a \cdot k_0 e^{\frac{-E_a}{RT}} \cdot C_{\rm CH_4} \tag{6}$$

$$k' = a \cdot k_0 e^{\frac{-E_a}{RT}} \tag{7}$$

The rate constant is combined with catalytic parameter "a" as follows:

$$a = [a_1][a_2][a_3] = \left[\frac{W_{cat}}{A_{ring}}\right] \left[\frac{A_{cat}}{W_{cat}}\right] \left[\frac{A_{ring}}{V_R}\right]$$
(8)

Substituting the previous values into the model (Eq. 6), the values of the rate constants k' and pre-exponential factor k_0 were determined, as summarized in Table 2.

Semi-pilot-scale packed bed reactor to study the effects of packing patterns

The ceramic Raschig ring catalyst had a single channel with an internal diameter of 0.55 cm, an external diameter of 1.2 cm, and a pellet length of 1.29 cm. The Raschig rings were packed in the reactor that was 10.16 cm in diameter and 5.16 cm long (see Fig. S4). The schematic diagram of the DMR for testing the Raschig ring catalyst on a semi-pilot-scale packed bed reactor is presented in Fig. S5. Two stainless steel plates were installed on both sides to create a set of realization of closely-packed packing. The reactor was placed in an electrically heated furnace with its temperature controlled by an intelligent temperature control meter (Carbolite modelVST12/600/3216P1). In order to explore the impact of structured Raschig ring catalyst packing in the reactor, three practical structured packing patterns, VS, CS, and RS, were modelled, as shown in Fig. 3.

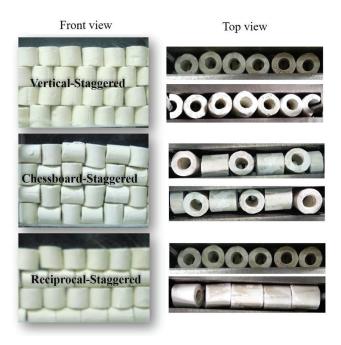


Fig. 3 – Three well-defined packing patterns

For a semi-pilot-scale system, H_2 with a flow rate of 150 mL min⁻¹ at 600 °C was used to reduce the catalyst for 12 h. The reactant gases (CH₄ and CO₂), controlled by a mass flow controller (Kofloc model 8500), were introduced through the Raschig ring packing bed balanced with N₂ with a feed reactant molar ratio (CO₂:CH₄:N₂) of 2:1:0.5. The conversion was measured by taking gas chromatography (GC) samples of the reactor effluents for 200 h. The carbon formation were investigated using the temperature programmed hydrogenation technique (TPH).

Results and discussion

Simulation results

Momentum transfer effects - velocity distribution

Changes in flow direction are forced by packing but remain under the governing laws of momentum, flow energy, and mass. Using COMSOL Multiphysics Version 3.5a, governing equations, and mathematical models, the hydrodynamics of the gas mixture were explained by the Navier-Stokes' equations:

$$-\rho(u \cdot \nabla)u = \nabla \cdot \left[-\eta \left(\nabla u + \left(\nabla u\right)^{T}\right)\right] = pI \quad (9)$$
$$\nabla \cdot u = 0 \quad (10)$$

The boundary conditions were set as follows: At inlet of reactor channel; $u \cdot n = v_0$, At wall of reactor channel; u = 0, At outlet of reactor channel; $p = p_{ref}$ in which the reference pressure at outlet was set to 101.325 kPa atmosphere.

Vertical staggered packing (VS)

For the VS packing pattern, twenty-four pellets were used to create four-row packing pattern, with the centers of each pellet being offset with the centers of the pellets in the following row, as shown in Fig. 4. The modelled volumetric flow rate of 576 mL min-1 was within the laminar flow regime adopted in the present work. Regarding velocity profile, flow velocity was highest at the centerline of the Raschig ring hole. This faster flow region occurred due to the small space between the external surface of the Raschig ring and the inner wall of the flow channel. Flow direction was mainly in axial direction. The flow was slow near the stagnation point at the bottom surface of the next Raschig ring row. There, the fluid stream divided and reemerged with the other half of the flow stream from the neighboring Raschig ring to ensure mass balance. A similar pattern to that of the first-row packing reappeared in the second and third rows of packing, as shown in Fig. 4. Nevertheless, average flow velocity was identical for each row.

Chessboard staggered packing (CS)

The CS packing pattern exhibited high flow on the vertical rings and very low flow velocity within the horizontal rings, as shown in Fig. 5. This higher flow velocity resulted from the reduction in the flow area due to packing, while the maximum velocity was higher than that of the VS packing pattern.

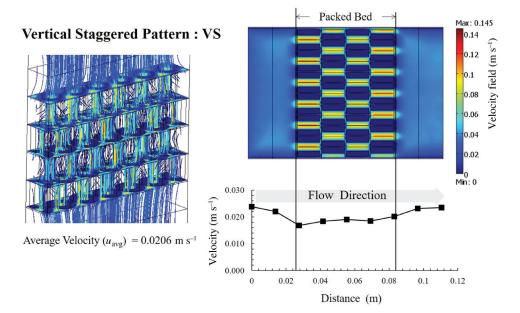


Fig. 4 – Total velocity distribution of VS packing

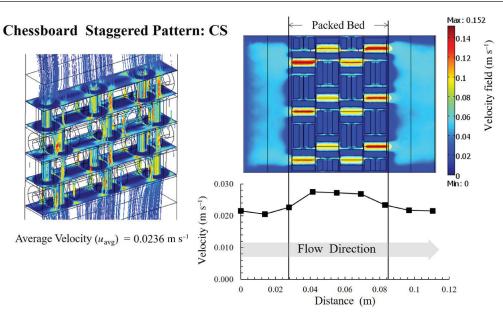


Fig. 5 – Total velocity distribution of CS packing

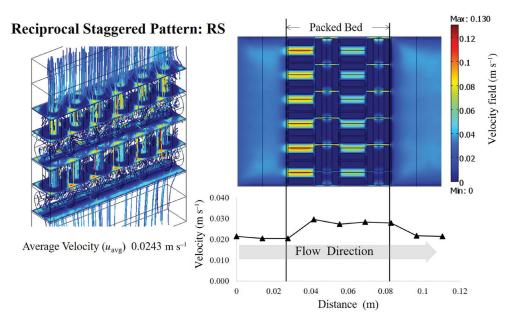


Fig. 6 - Total velocity distribution of RS packing

Reciprocal staggered packing (RS)

The flow structure observed within the first row of the RS pattern was qualitatively the same as that of the VS packing pattern. The changing of Raschig ring direction influenced the flow in the second row. The gas moved from axial direction to radial direction. In the third row, the gas changed direction again to axial. Therefore, there was more variation in flow distribution in the RS packing pattern than in the other patterns. This packing pattern offers both radial mixing and axial mixing, as shown in Fig. 6. The influence of different packing patterns is illustrated in Fig. S6. The reactors demonstrated an entry length zone and a reaction zone. In the entry length zone, reactants were mixed before flowing through the catalyst pack, shown at a distance from the inlet of 0 to 0.028 m.

For the reaction zone, the reactants contacted the catalyst to transform into product molecules, shown at a bed distance from 0.028 to 0.083 m. The VS packing pattern produced the lowest velocity distribution, where the flow was mainly in axial direction. The CS and RS patterns, where the packing was a mixed horizontal and vertical ring inside the bed, exhibited similar velocity distributions. However, the RS packing pattern obtained the highest velocity distribution due to the horizontal direction of the rings, with more horizontal rings decreasing the bulk area in the second and fourth rows.

Momentum transfer effects – pressure drop

The results indicate that pressure drop was influenced by particle arrangement, which can be evaluated using the CFD models, as shown in Fig. S7. Pressure drop was especially significant in the horizontal Raschig ring direction. The VS pattern produced the lowest pressure drop among the studied patterns. The RS pattern exhibited the highest pressure drop with respect to the other two patterns, and tended to increase much faster along the bed. In general, pressure distribution was quite uniform in each row of catalyst across the studied patterns, with the exception of RS, for which the entrance effect and flow impingement may have somehow affected pressure near the center of the reactor, causing it to be lower than that near the side. In addition, the pressure field revealed two-value distribution for each row of packing using the RS pattern, i.e., the higher the pressure within horizontal catalyst pellets, the lower the pressure within vertical catalyst pellets. This is in accordance with the inverse velocity distribution and in compliance with the energy principle.

It is evident that variations in local velocity and fluid pressure were significantly affected by packing pattern (see Table 3). The pressure drop across a Raschig ring bed is typically attributed to several factors, including bounding wall viscosity, catalytic domain, and inertia force.

The VS pattern is a well-known industrial pattern that has been validated with an average velocity of 0.0207 m s⁻¹ and pressure drop of 223 mPa. Adjusting the average fluid velocity or resident time inside the low tube-to-particle packed bed can be done not only by changing the bed volume, but also by using different packing patterns. The CS pattern creates more local turbulence by placing horizontal rings within every row in the bed. The same number of horizontal rings has been modelled in two rows between the vertical rows in a RS pattern.

 Table 3 – Comparison of average velocity via pressure drop in three packing patterns

Packing pattern	Average velocity $u_{av} [m \ s^{-1}]$	Pressure drop Δp [mPa]
Vertical staggered: VS	0.0207	223
Chessboard staggered: CS	0.0237	228
Reciprocal staggered: RS	0.0243	308

The results indicate that the local turbulence promoted in a CS pattern can reduce average fluid velocity when compared to the VS pattern.

Heat transfer effect

Since the DMR is highly endothermic, the combination of momentum, heat, and mass transfer is important in terms of packing geometry. The energy balance equation applied to the packed bed reactor domain in consideration of heat transfer through convection and conduction, was as follows:

$$\rho C_p \frac{\partial T}{\partial t} + \nabla \cdot \left[-k_D \nabla T \right] + \rho C_p u \cdot \nabla T = Q \quad (11)$$

The temperature gradient profile due to the DMR reaction can be seen in Fig. S8. In comparison, the VS pattern exhibited the lowest average temperature at 548 °C, while the CS pattern exhibited the highest average temperature at 558 °C, and RS pattern exhibited an average temperature of 555 °C during the DMR process. Notably, the furnace must reach 600 °C to support the reaction temperature. Notably, Raschig ring direction can control fluid flow direction and heat distribution (discussed in more detail in the next section).

Figs. S9a, S9b and S9c show insignificant overall temperature variation along the reactor height within the Raschig ring packing during DMR. The inlet temperature and wall temperature were set to 600 °C. There was a sharp temperature decrease within a limited region between the first row of packing and above the catalyst entrance level. This was mainly due to heat being consumed by the DMR process, which is slightly endothermic. Due to the endothermic reactions, the temperature inside the bed decreased. Moreover, there were strong axial and radial heat differences of up to approximately 40-50 °C. A nearly uniform temperature distribution was obtained within the medium zone of the packing bed. As previously mentioned, Raschig ring direction is one of the primary determinants of flow distribution. During the reaction, the temperature was high at the entrance and dramatically dropped in the medium zone, depending on the packing pattern used. Upon comparing the three packing patterns, the VS pattern facilitated the highest flow velocity at the centerline of the hole, with temperature distribution being in a largely axial direction. Therefore, the overall temperature for the VS pattern was lower than that of the other patterns.

Mass transfer effect

As previously stated, the goal of the present research was to study the effects of packing pattern on DMR reactions. The results of CFD modelling can provide microscopic data that may be difficult to measure experimentally, especially when considering a semi-pilot-scale processing unit. As expected, both reactants (CH₄ and CO₂, appeared in high concentrations at the entrance of the bed and then became consumed as they decreased towards the bottom (see Figs. S10 and S11). Hydrogen and carbon monoxide (H₂ and CO) both appeared in high quantities at the bottom (see Figs. S12 and S13).

Figs. S10 and S11 clearly present the distribution of CH_4 and CO_2 concentration along the packing bed for the different packing patterns. Notably, CH_4 and CO_2 concentrations decreased due to the DMR reaction. The VS pattern showed lower concentrations of CH_4 and CO_2 over the reactor length, implying the highest rates of CH_4 and CO_2 conversion. However, the results suggested differences between the simulation and the experiment. In this case, this effect may be explained in terms of carbon deposition. Regarding the rate equation mechanism and kinetic model, this model did not cover overall surface species effects in which catalyst deactivation was mainly caused by carbon deposition. It is discussed in more detail in the next section.

Analysis of DMR reaction over Raschig ring packing catalyst

 CH_4 conversion values for VS, CS, and RS patterns were 75.97 %, 73.80 %, and 74.25 %, respectively, while the average percent errors were in the 6–10 % range for the three packing patterns. The

product ratio of H_2/CO was >1 for all packing patterns. The results indicate that the effects of packing pattern can be investigated further regarding CH_4 decomposition, which is directly affected by DMR.

Fig. 7 shows the % CH_4 conversion, % CO_2 conversion values, and % H, and % CO selectivity as a function of time for 200 h. It was determined that packing pattern influenced the time required for the system to reach a relationally steady value of % CH₄ conversion. Namely, it took 21 h, 3 h, and 2.17 h for reaction systems with VS, CS and RS packing patterns to reach a steady value of % CH₄ conversion at 75.97 %, 73.80 %, and 74.25 %, respectively. Similarly, it was determined that packing pattern influenced the time required for the system to reach a steady value of % CO₂ conversion. Namely, it took 42.6 h, 53.17 h, and 9.17 h for reaction systems with VS, CS and RS packing patterns to reach a steady value of % CO₂ conversion at 20.05 %, 13.09 %, and 11.65 %, respectively. In contrast to % CH₄ and % CO₂ conversion, H₂ and CO selectivity continuously changed over the 200-h operation. It was found that the packing patterns remarkably influenced the selectivity. Significantly, H, selectivity continued to increase from 55.37 % to 70.30 % in the first 28.3 h, and from 70.30 % to 81.09 % from 28.3 h to 200 h. A possible explanation for the continuous increase in H₂ selectivity was the occurrence of coke formation on the catalyst, which caused the decomposition of CH₄ into coke and H₂.

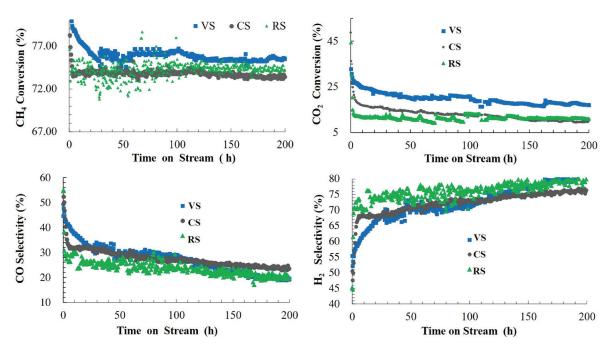


Fig. 7 – DMR performance of VS, CS, and RS packing patterns for DMR reactions at 600 °C, feed composition CH_4 : $CO_2 = 1:2$

Effects of packing pattern on coke formation

Due to the hotspot issues inherent in packed columns, coke can easily form on a catalyst surface under the decomposition reaction. As seen in Fig. S14, the TPH was used to investigate the types of coke formed.

 H_2 gas was introduced into the reactor with a flow rate of 40 mL min⁻¹ from 27 °C to 900 °C. The gas effluent (CH₄) was then collected to investigate coke formation on the surface of Raschig rings following Eq. 12:

$$C+2H_2 \longrightarrow CH_4$$
 (12)

Morris and Calvin²⁹ reviewed information on the type of coke that formed when using a Ni catalyst. The VS pattern exhibited two types of coke deposition on the Raschig ring surface, namely whisker-like and pyrolytic carbon (at temperatures between 400 – 600 °C or greater).

The TPH profiles of the CS and RS patterns retained two types of coke on their surface at temperatures between 350 - 400 °C and 400 - 450 °C, presented as encapsulating film and whisker-like carbon. These carbon types express slow polymerization of CH₄ radicals on the Raschig ring catalyst surface, forming encapsulating film and some whisker-like growth, as shown in Figs. 8 and 9. The CS and RS patterns introduced more local turbulence due to the placement of horizontal rings. Table 3 presents the average velocity results, which were lower in the CS and RS than in the VS pattern. Therefore, the pyrolytic carbon type disappeared in the CS.

Notably, the types of coke formation present on a catalyst surface depended significantly on the packing patterns due to variations in their contact time and temperature in the beds. A suitable pack-

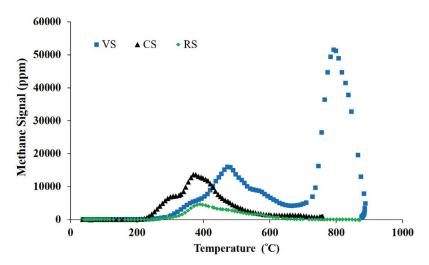


Fig. 8 – TPH results for Raschig ring packing after the semi-pilot-scale packed bed DMR process

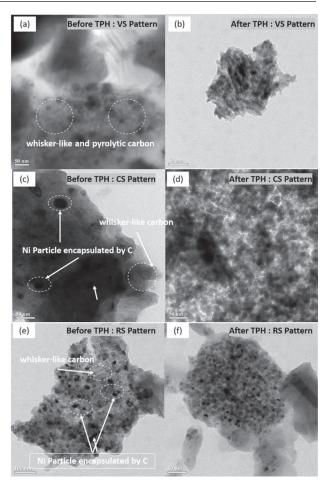


Fig. 9 – TEM images of (a) and (b) VS; (c) and (b) CS; (e) and (f) RS

ing pattern could be useful in helping to reduce the polymerization of carbon deposition onto a catalytic surface since the lifespan of the catalyst depends on coke formation. Steady-state operation and the energy balance around control volume are explained in Fig. 10. The energy conservation of the bed con-

sists of the enthalpy in and out with inlet and outlet streams $(\dot{F}_{in}\dot{H}_{in},\dot{F}_{out}\dot{H}_{out})$ the energy transfer from furnace via the reactor wall (\dot{Q}) , and the energy consumed by the endothermic reaction $(F\dot{x}_i\Delta H_{ren})$.

$$\dot{F}_{in}H_{in} - \dot{F}_{out}H_{out} + + UA\Delta T_{im} - \dot{F}x_i\Delta H_{rxn} = 0$$
(13)

The bed may be considered isothermal at any given time with the overall temperature level increasing with time of operation, in which the number of moles in more or less equals that of the moles out, the inlet stream (\dot{F}_{in}) is not much different from outlet stream (\dot{F}_{out}) and the inlet temperature (T_{in}) is equal to the outlet temperature (T_{out}) due to isothermal; therefore:

$$UA\Delta T_{lm} = \dot{F}x_i \Delta H_{rxn} = \dot{Q}_{rxn} \tag{14}$$

In the case that the three packing patterns return more or less the same value of conversion (see Table 4), this $(F\dot{x}_i\Delta H_{rxn})$ can be taken as the same constant. The UA value can be calculated from the experimental data. The overall heat transfer coefficient can be calculated as shown in Eq. 14.

$$\frac{1}{U} = \frac{1}{h_{fluid}} + R_{cond} + \frac{1}{h_r}$$
(15)

The VS pattern resulted in the highest temperature coke type. This was due to the most efficient heat transfer of this pattern, as seen by the highest coefficient of $UA = 1.50 \cdot 10^{-1}$ W m⁻² K⁻¹ in Table 4. The TPH shows carbon films at a high temperature starting polymerization into the whisker-like and pyrolytic carbon phases.

A summary of the effects of the three packing patterns on pressure drop, heat transfer efficiency,

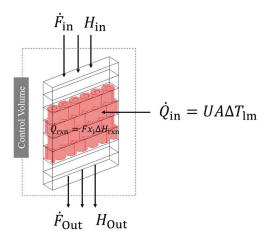


Fig. 10 – Control volume for the energy balance

Table 4 – Summary of the overall heat transfer coefficient results

Packing patterns	Equations	$\begin{bmatrix} UA \\ W m^{-2} K^{-1} \end{bmatrix}$
Vertical staggered: VS	$\dot{Q}_{rxn} = (UA\Delta T_{lm})_{Vertical}$ (16)	$1.50 \cdot 10^{-1}$
Chessboard staggered: CS	$\dot{Q}_{rxn} = (UA\Delta T_{lm})_{\text{Chessboard}}$ (17)	$1.46 \cdot 10^{-1}$
Reciprocal staggered: RS	$\dot{Q}_{rxn} = (UA\Delta T_{lm})_{\text{Reciprocal}}$ (18)	$1.44 \cdot 10^{-1}$

reaction conversion, and amounts of coke deposit is presented in a radar chart (Fig. 11). For the VS packing pattern, which contained a total of 24 pellets in a vertical direction, the results of momentum transfer showed the lowest pressure drop (223 mPa) compared to the other patterns. For heat transfer during the DMR reaction using the required thermal capacity (UA value), the vertical direction largely observed with the VS pattern was applied in a mainly conductive manner rather than convective. The fluid flowed mostly in an axial direction and the VS pattern exhibited the highest UA value of $1.50 \cdot 10^{-1}$ W m⁻² K⁻¹. Additionally, the VS pattern exhibited the highest rate of CH_4 conversion (75.97 %). For the CS pattern, which contained 22 pellets in total, more local turbulence was produced by placing horizontal rings within every row in the bed. The results of momentum transfer showed a pressure drop of 228 mPa. Regarding heat transfer during the DMR reaction, the results for this pattern were lower than those of the RS pattern, but higher than the VS pattern in terms of UA value. Additionally, the effects of mass transfer in the form of coke deposition were lower than for the VS pattern, but higher than for the RS pattern. Moreover, the CS pattern exhibited reduced CH_4 conversion (73.80 %) com-

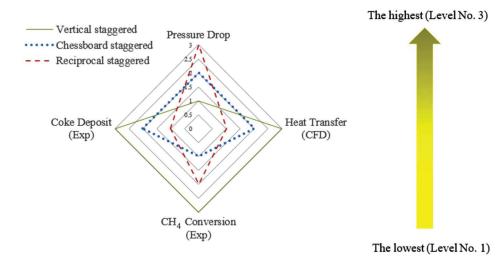


Fig. 11 – Radar chart for the effects of packing pattern on pressure drop, heat transfer, CH_4 conversion, and coke deposition

pared to the other patterns. Finally, the RS pattern, contained 22 pellets in total as mixed horizontal and vertical rings inside the bed. For momentum transfer, the results indicated that this pattern exhibited the highest pressure drop (308 mPa). Regarding heat transfer effects, this pattern exhibited the lowest heat transfer due to the DMR reaction, while also exhibiting the least amount of coke decomposition on the catalyst surface.

Conclusions

Three packing patterns, VS, CS, and RS, were investigated according to the low tube-to-particle diameter ratio (N = 4-8). Both numerical and experimental methods were used to investigate the pressure drop, heat transfer, CH₄ conversion in the DMR process. The lowest pressure drop of 223 mPa was observed in the VS packing pattern because the Raschig rings were placed in vertical direction. This

faster flow (mainly in an axial direction) occurred due to the small space between the external surface of the Raschig ring and the inner wall of the flow channel. The highest thermal capacity was observed for the VS pattern ($UA = 1.50 \cdot 10^{-1} \text{ W m}^{-2} \text{ K}^{-1}$). This can be explained by the vertical direction being mainly conductive rather than convective. Moreover, the highest level of CH₄ conversion was observed in VS packing (75.97 %). Unfortunately, VS packing exhibited the highest level of coke formation. This was evidenced by the carbon type pyrolytic and whisker-like carbon present on the surface of Raschig rings. However, a delicate catalyst packing pattern interplay can be achieved by means of a precise, holistic, and consistent understanding of the DMR process. The methodology presented in this research can also be used to provide design data for other reactions, so that a chemical engineer can prepare for the effects of packing patterns in the case of a low tube-to-particle diameter ratio reactor.

Supplementary materials

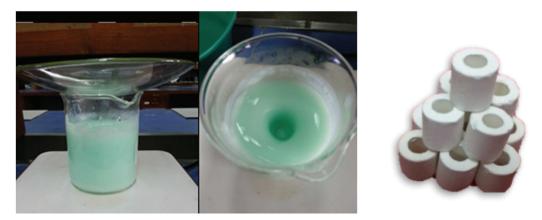


Fig. S1 – Schematic diagram of the catalyst coating on the wall surface of the Raschig ring

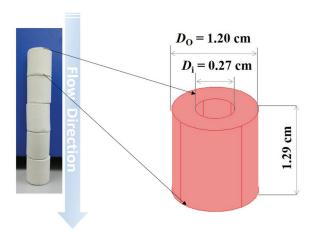


Fig. S2 – Dimensions of Raschig rings

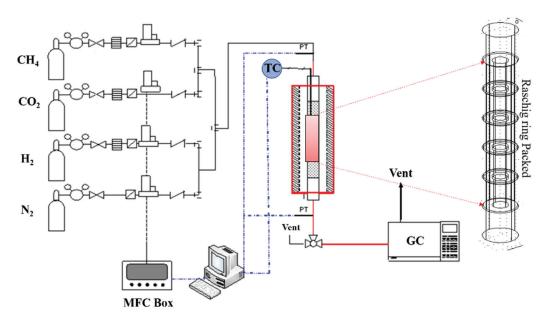


Fig. S3 – Schematic diagram of the DMR system

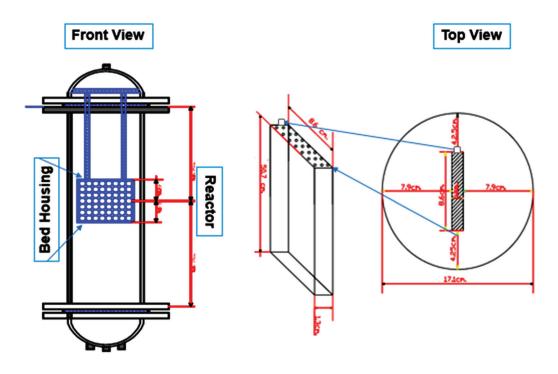
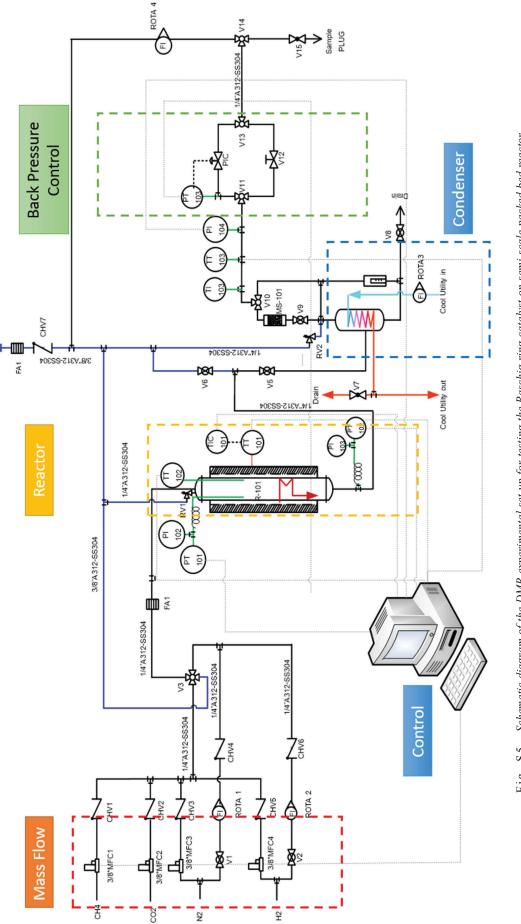


Fig. S4 – A semi-pilot-scale packed bed reactor



VENT

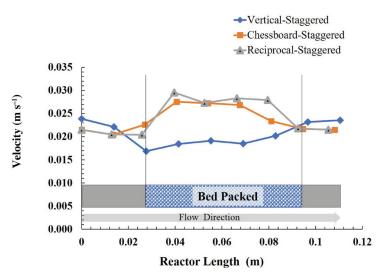


Fig. S6 – Velocity distribution profile for each packing pattern

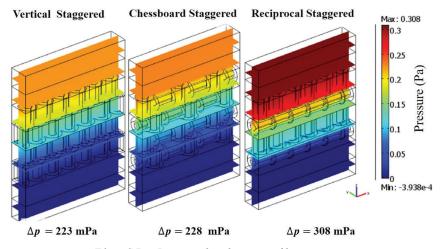


Fig. S7 – Pressure distribution profile

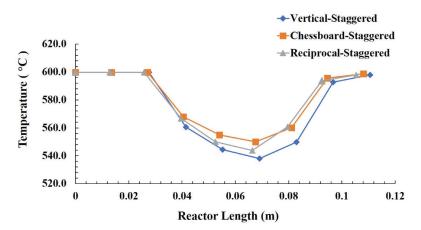


Fig. S8 – Temperature gradient in different Raschig ring positions during DMR process

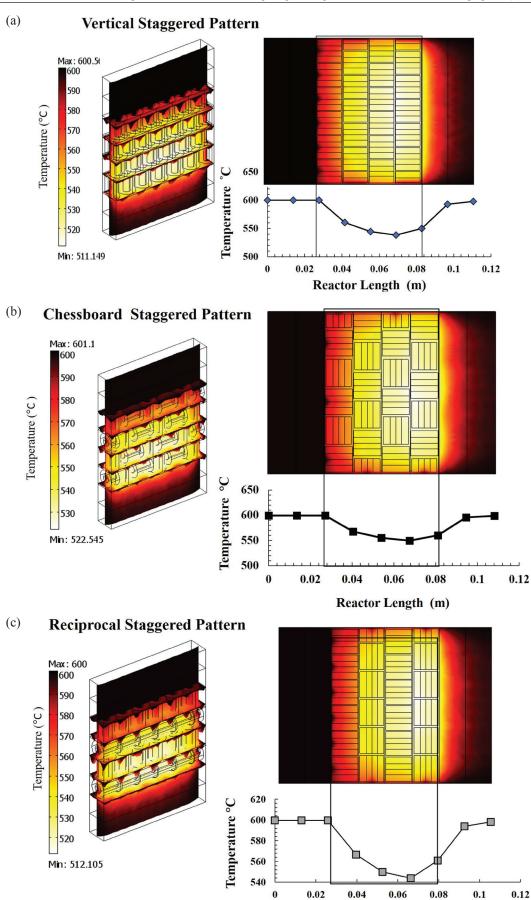
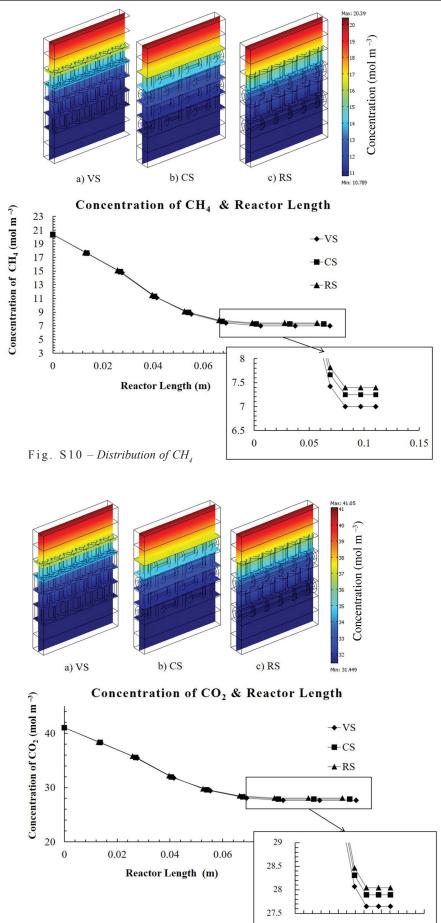


Fig. S9 – Temperature gradient of Raschig ring packing during the DMR

Reactor Length (m)

206



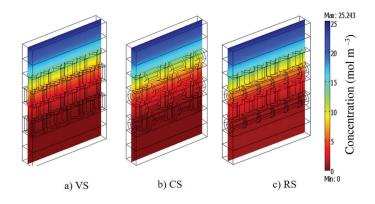
0

0.05

0.1

0.15

Fig. S11 – Distribution of CO_2



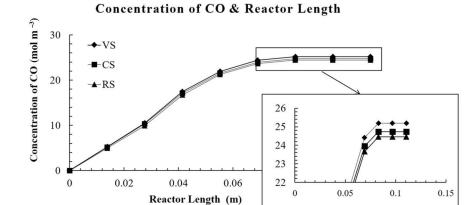
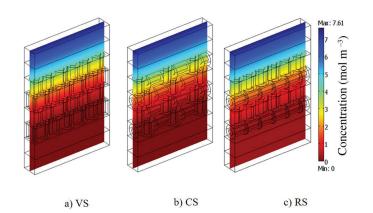


Fig. S12 – Distribution of CO



Concentration of H₂ & Reactor Length

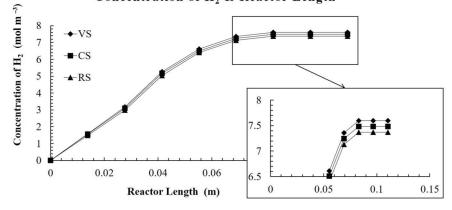


Fig. S13 – Distribution of H_2

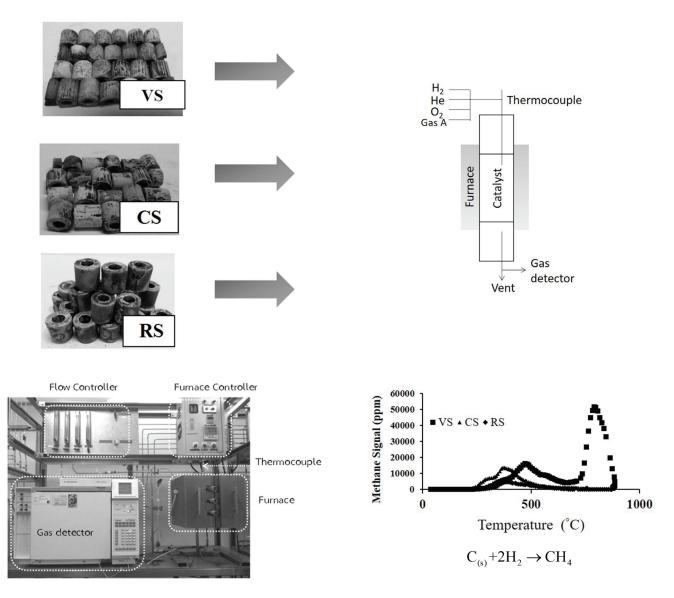


Fig. S14 – Experimental set-up for determination of coke formation on catalytic surface

J

 r_i

 C_{i}

З

а

 V_{R}

 A_{cat}

 a_1

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List of symbols

- k_0 pre-exponential factors, m s⁻¹
- k' rate constant
- E_a activation energy, J mol⁻¹
- m reaction order of CH_4
- n reaction order of CO₂
- Δp pressure drop, mPa

- UA heat transfer coefficient, W m⁻² K⁻¹
 - objective function
 - rate equation of species *i*
 - concentration of species *i*, mol dm⁻³
- $C_{i_{model}}$ molar concentration of species "*i*" from COMSOL model, mol dm⁻³
- C_{i_exp} molar concentration of species "*i*" from experiment, mol dm⁻³
 - tolerance
 - catalyst characteristic parameter
- W_{cat} weight of catalyst on Raschig ring surface, g
 - reactor volume, m³
 - surface area of a catalyst, m²
- A_{ring} surface area of Raschig ring, m²
 - catalyst weight per unit area of Raschig ring surface, m³ g⁻¹

- a_2 catalyst loading on Raschig ring surface, m² g⁻¹
- a_3 surface area of Raschig ring per unit volume, m² m⁻³

 ρ – density, kg m⁻³

- u velocity, m s⁻¹
- η viscosity, kg m⁻¹ s⁻¹
- p pressure, Pa
- p_{ref} reference pressure, Pa
- $k_{\rm D}$ thermal conductivity, W m⁻¹ K⁻¹
- \dot{F}_{in} inlet stream
- F_{out} outlet stream
- T_{in} inlet temperature, °C
- T_{out} outlet temperature, °C
- h_{fluid} heat transfer coefficient, W m⁻² K⁻¹
- N = 1 low tube-to-particle ratio (d_t/d_p)
- d_{i} reactor diameter (m)
- $d_{\rm p}$ catalyst diameter (m)

Abbreviations

- VS vertical staggered
- CS chessboard staggered
- RS reciprocal staggered
- CFD computational fluid dynamics

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